



Heavy quarks and quarkonia production in high energy experiments

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Heavy quark production: phenomenological framework



$$\frac{d\sigma}{dX} = \sum_{j,k} \int_{\hat{X}} f_j(x_1, Q) f_k(x_2, Q) \frac{d\hat{\sigma}_{jk}(Q)}{d\hat{X}} F(\hat{X} \rightarrow X; Q)$$

Factorization formula

- Parton PDF's $f(x, Q)$ (universal)
- The cross section for the scattering of the partons j, k , computed in *perturbative* series pQCD at next to leading order (NLO) in α_s .
- A fragmentation function for the transition to the final state. Includes long-distance effects, taken as universal (e.g., from $Z \rightarrow b \bar{b} \rightarrow B X$)
- Q here stands for the mass scales that come into play:
 - Factorization scale
 - Heavy quark mass
 - Renormalization scale
 - p_T scale
- For $p_T \approx m_Q$, the parton cross section is computed for massless light quark [u, d, s (c)] and g, and heavy b
- For $p_T \gg m_Q$ the b quark becomes an active contributor (its mass may be neglected)

Merging low- p_T and high- p_T regions, analytical computations:

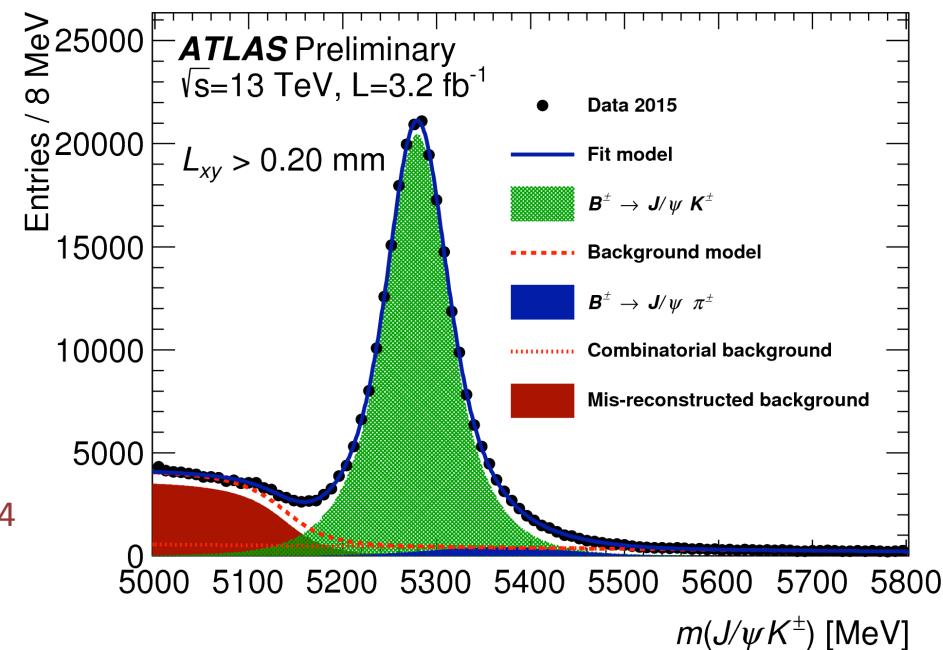
- The General Mass - Variable Flavor Number Scheme (GM-VFNS): similar to methods used in deep inelastic scattering, with NLO and next leading log (NLL) accuracy.
- The Fixed Order plus Next Leading Log (FONLL) scheme, with an empirical matching function for the NLO massive (low p_T) and massless (high p_T) ranges.

The MC generators:

- PYTHIA, HERWIG: LO+LL computation allowing detailed description of the final states
- MC@NLO, POWHEG, MADGRAPH: modeling of the hard scattering, generally NLO + LL, interfaced with the the generators above for parton PDFs and hadronization.

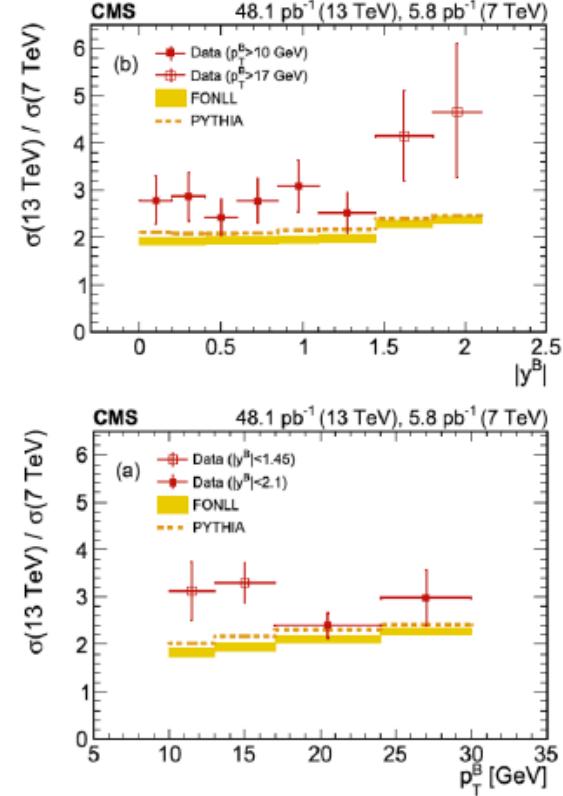
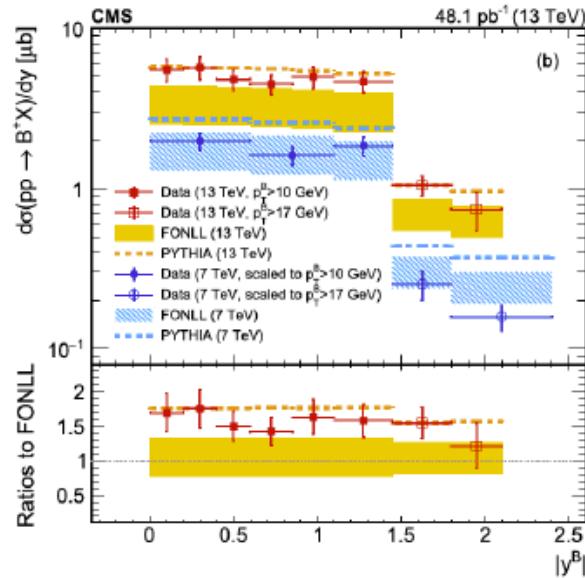
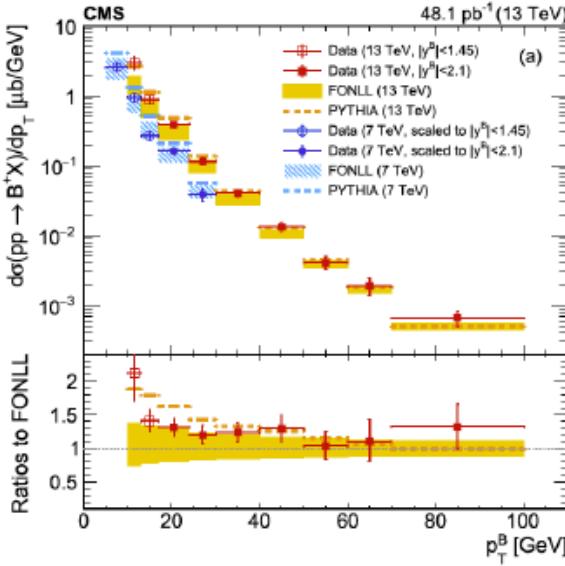
Results on B hadron production at LHC

- B^+ differential cross section is the most direct process, in particular for ATLAS and CMS:
 - Decay channel $J/\psi K^\pm \rightarrow \mu^+ \mu^- K^\pm$
 - Selection via muon pairs and displaced vertices
 - Similar techniques used for:
 - $B^0 \rightarrow J/\psi K^{*0} \rightarrow \mu^+ \mu^- K^+ \pi^-$ (ATLAS has measured the ratio of $\sigma \times BR$)
 - $B^0 \rightarrow J/\psi K_S \rightarrow \mu^+ \mu^- \pi^+ \pi^-$ and $B^0_S \rightarrow J/\psi \phi \rightarrow \mu^+ \mu^- K^+ K^-$ (used for studies of decays)



ATLAS-CONF-2015-064

B⁺ cross section at 13 TeV with CMS



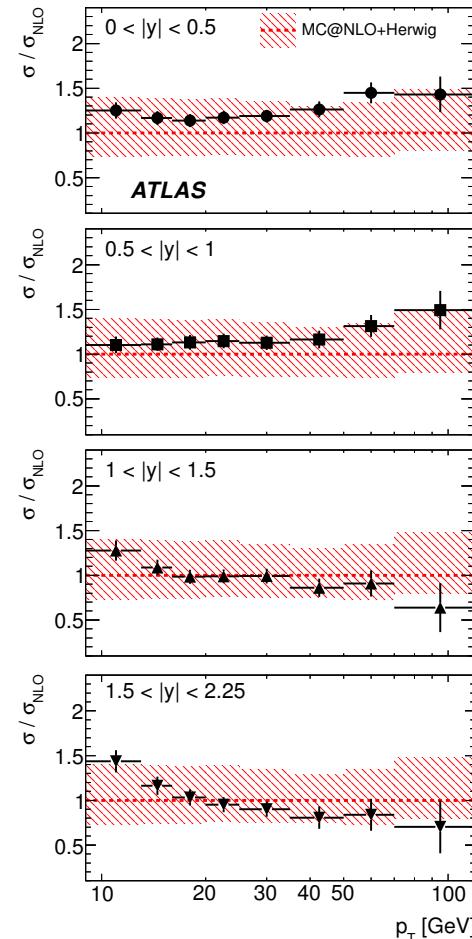
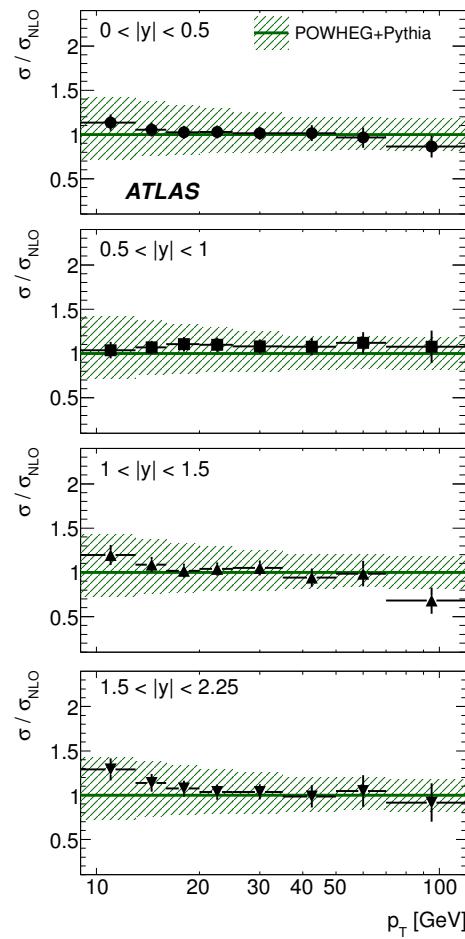
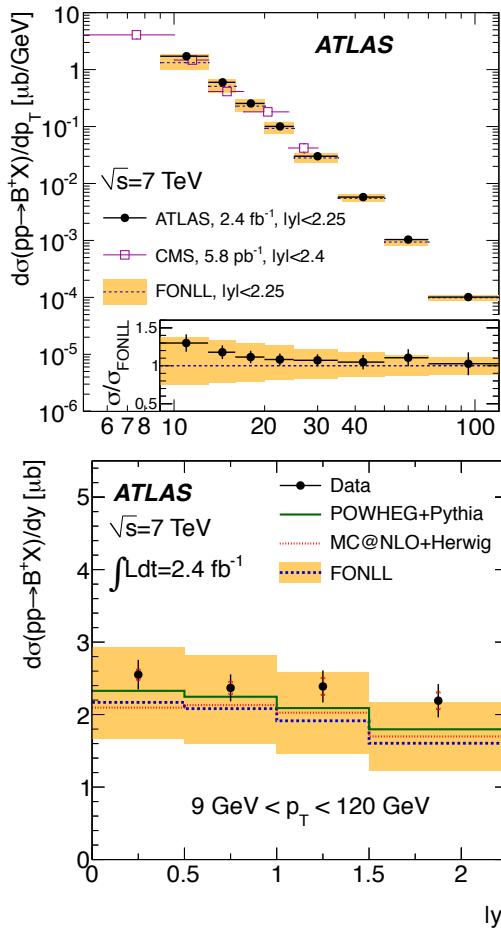
- Shape and normalisation in reasonable agreement with FONLL and PYTHIA
- 13 to 7 TeV ratio tend to prefer higher values wrt predictions

Phys. Lett. B771 (2017) 435 ([arXiv:1609.00873](https://arxiv.org/abs/1609.00873))

B⁺ cross section at 7 TeV (ATLAS)

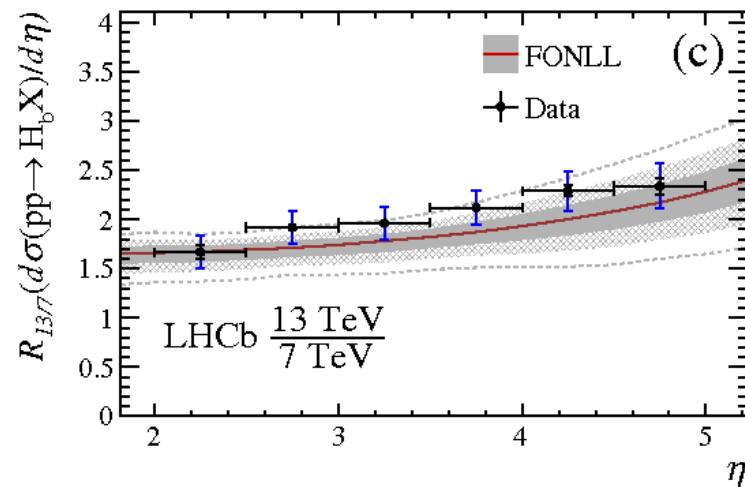
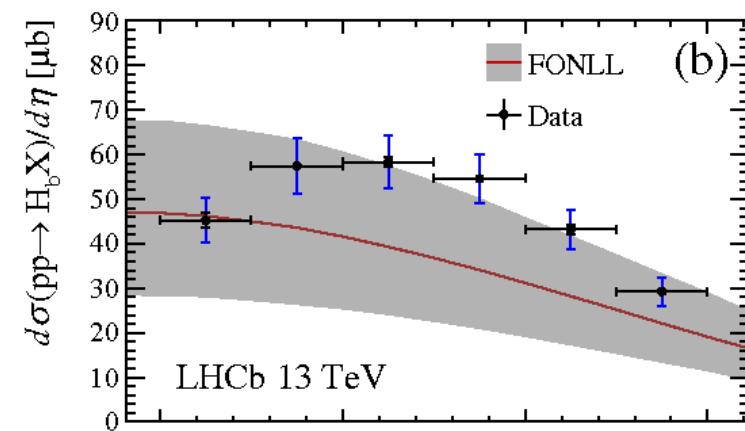
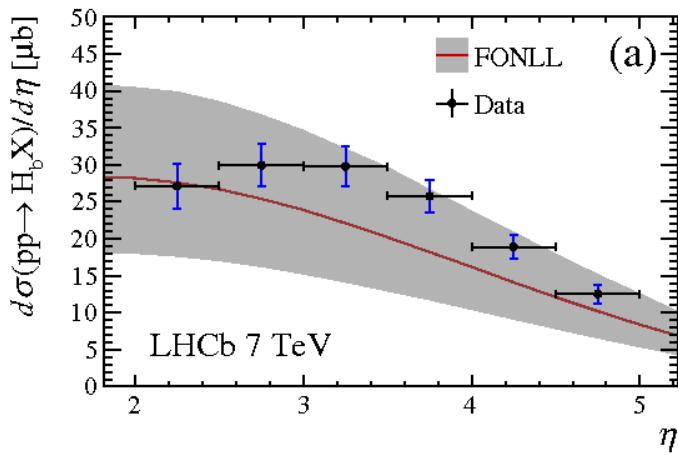
A comprehensive comparison of data and the different predictions was performed by ATLAS at 7 TeV.

JHEP 10 (2013) 042



Inclusive B production with LHCb

This is an inclusive search for $H_b \rightarrow H_c \mu^- X$ in the forward region. The c -hadron may be D^0 , D^+ , D_s^+ , or Λ_c , in a fully reconstructed hadronic decay.

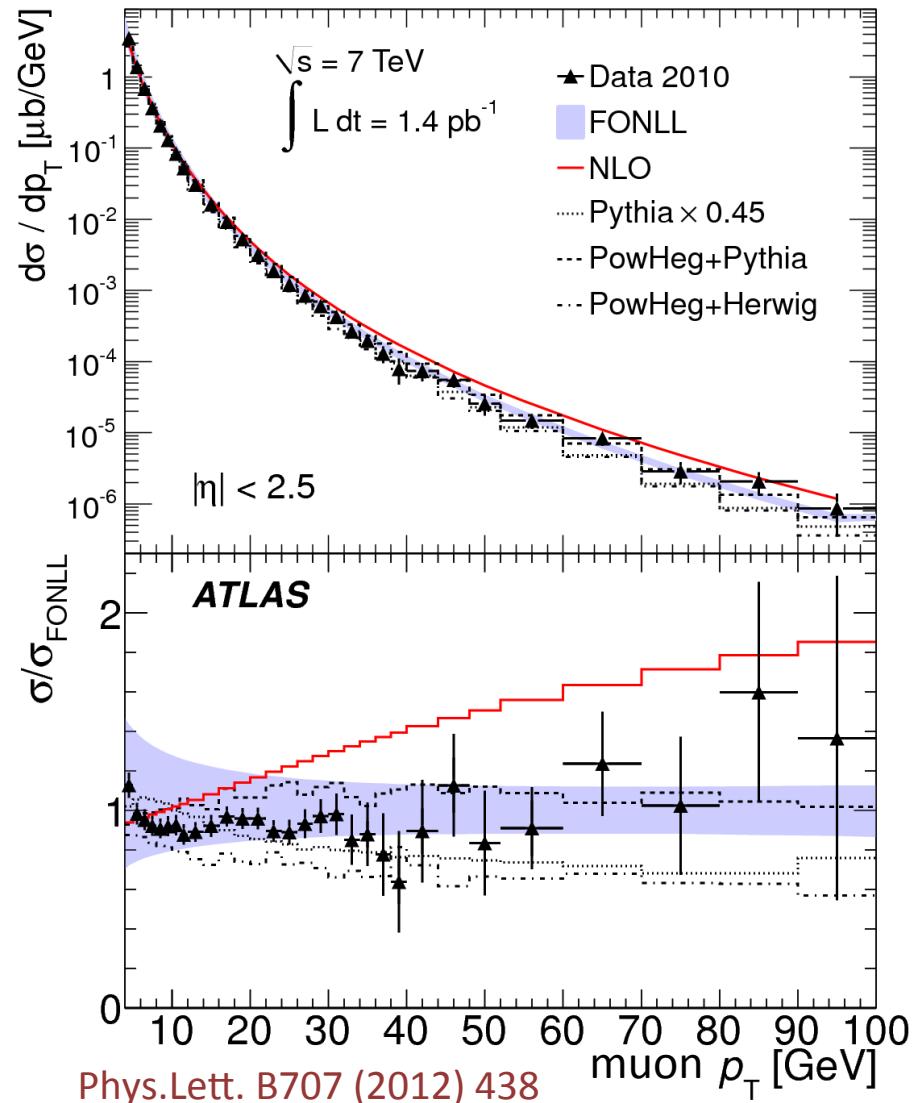


Phys. Rev. Lett. 118, 052002 (2017)
[arxiv:1612.05140](https://arxiv.org/abs/1612.05140)

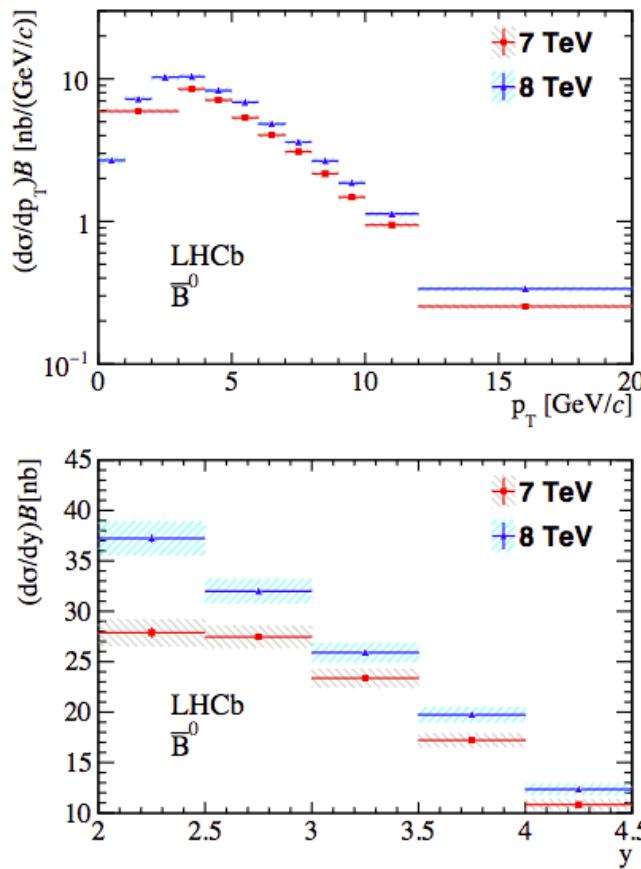
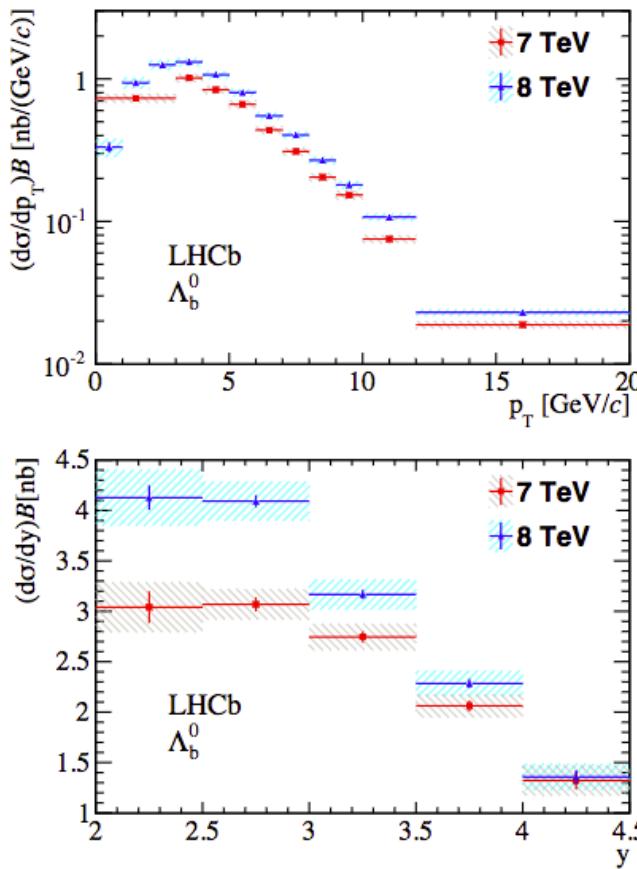
Lepton momentum spectrum

$H_b + H_c$ production at high p_T can be related to the spectrum of muon from inclusive decays. ATLAS and CMS can reach large values of p_T .

An early measurement of the spectrum of $p_{T\mu}$ from a few GeV to 100 GeV. The plot shows explicitly the effect of the NLL component in FONLL.



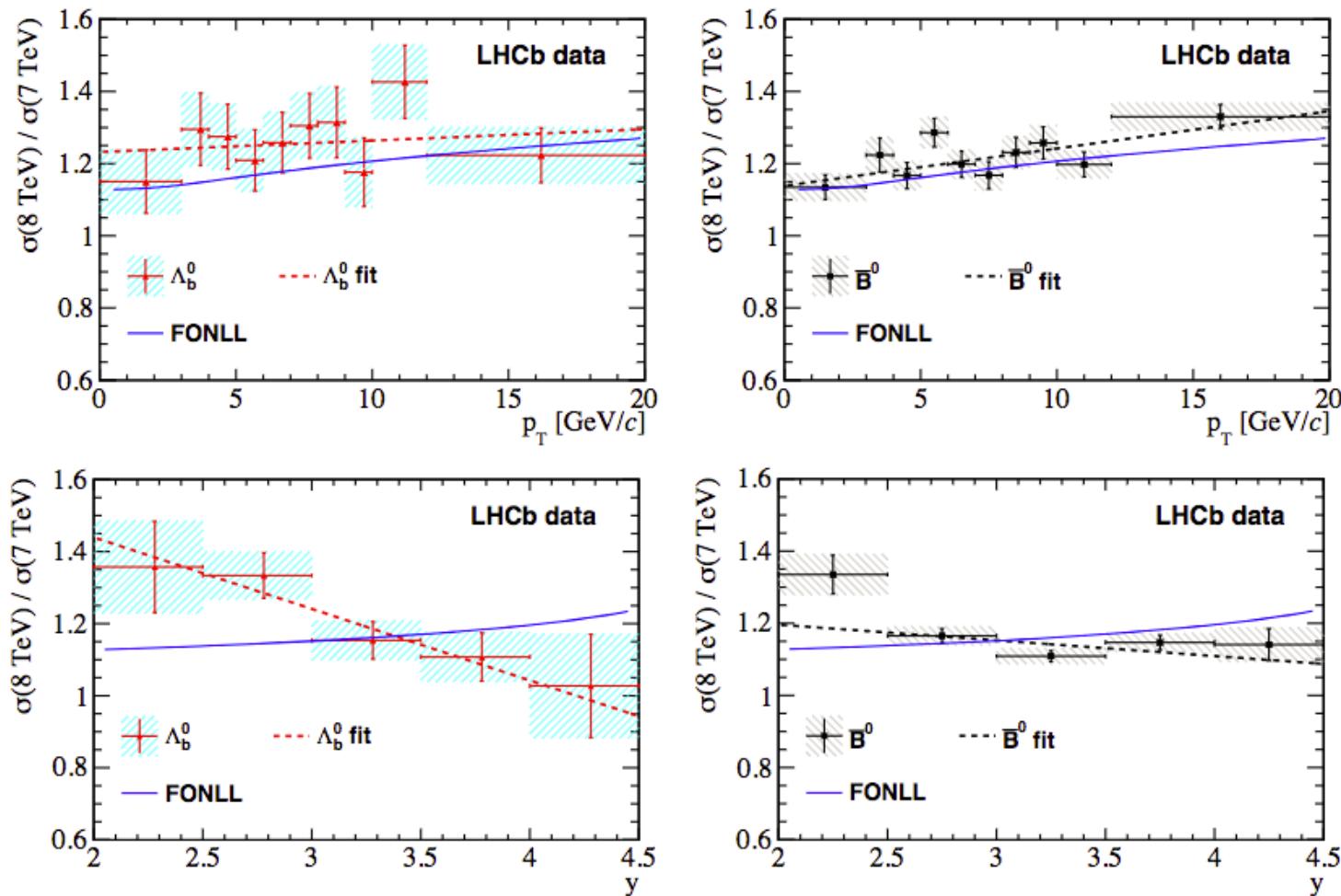
Λ_b and B^0 production with LHCb



Chin.Phys. C40, n.1
 (2016) 011001
[arXiv:1509.00292](https://arxiv.org/abs/1509.00292))

CMS at 7 TeV in Phys.Lett. B714 (2012)136)[arXiv:1205.0594](https://arxiv.org/abs/1205.0594))

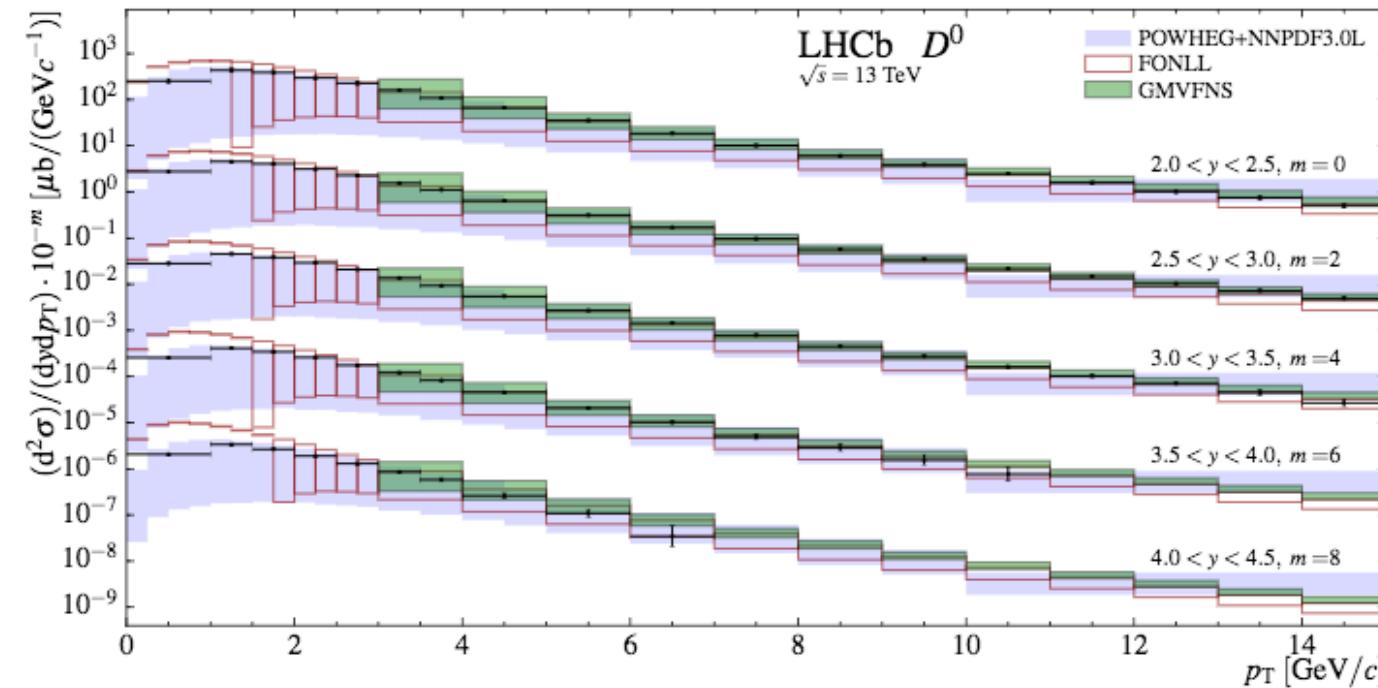
Λ_b and B^0 production with LHCb – continued



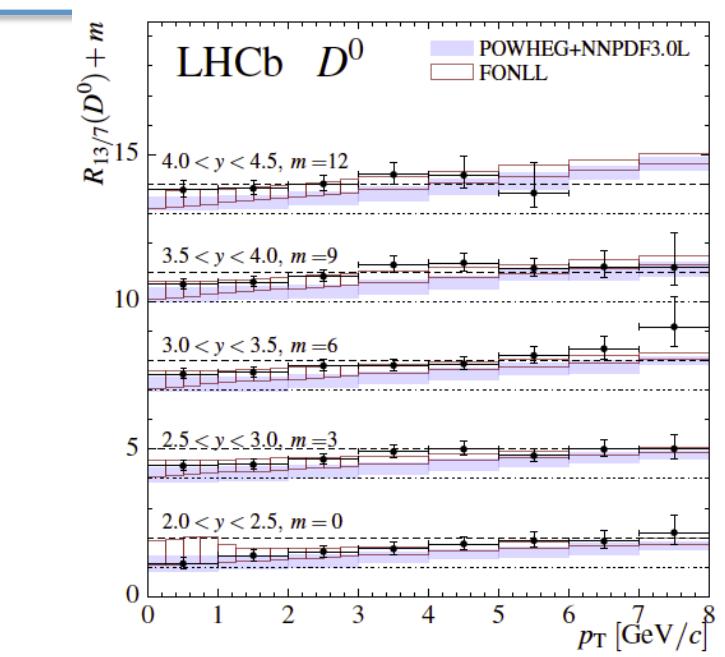
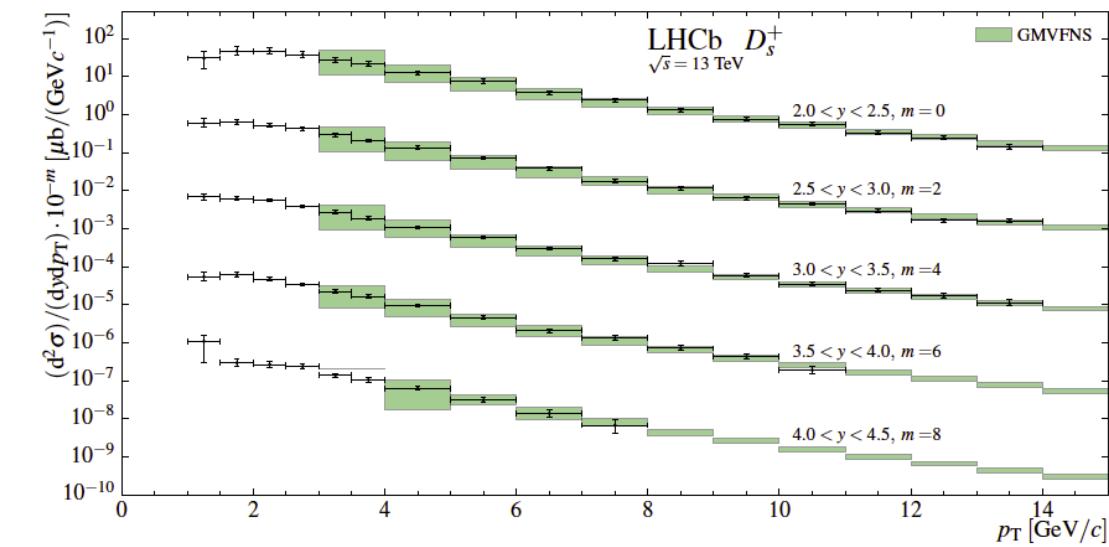
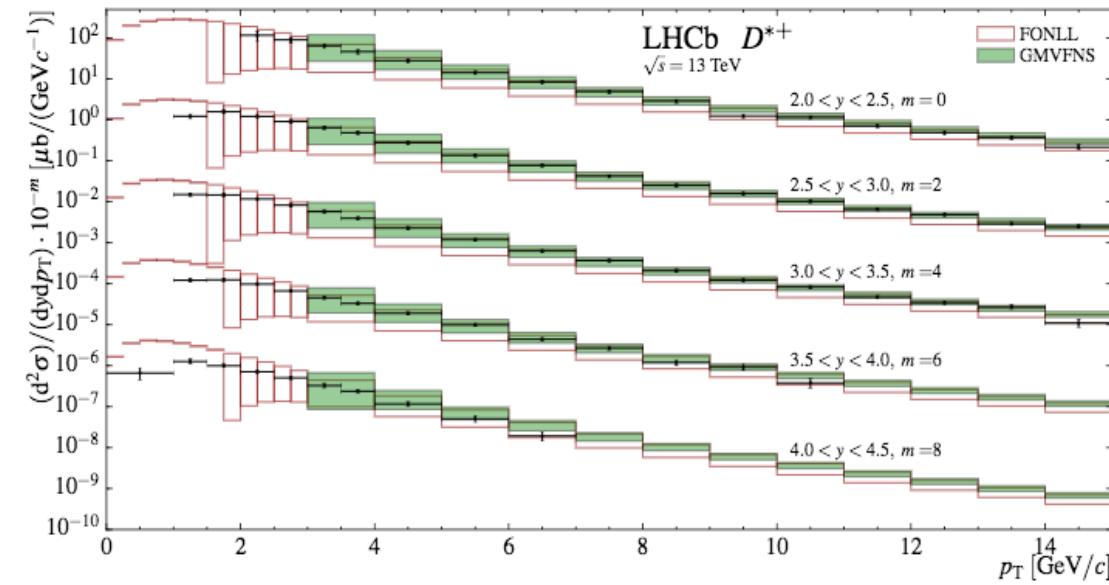
Deviation from FONLL prediction in the y dependence.

Charm production with LHCb

- LHCb studies HQ production in the region $2 < y < 4.5$ and $p_T < 15$ GeV.
- Few-body decays are reconstructed from secondary vertices are reconstructed, with hadron identification and no need for leptons.
- Charm production has been studied for D^0 , D^+ , D^+_S and D^{*+} .



- D mesons from B decays are removed,
- Forward production is sensitive to $x_F < 10^{-4}$, these measurements contribute to the determination of the gluon PDF



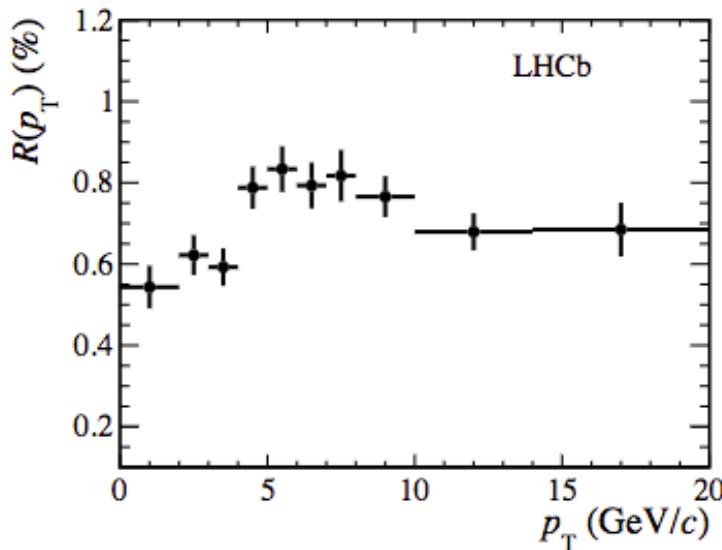
Ratio of differential cross sections at 13 TeV over 7 TeV, with offsets (lines corresponds to equal value and factor 2 increase).

Charm production also at 5 TeV (LHCb)
in JHEP 02 (2014) 072 ([arXiv:1308.6729](https://arxiv.org/abs/1308.6729))

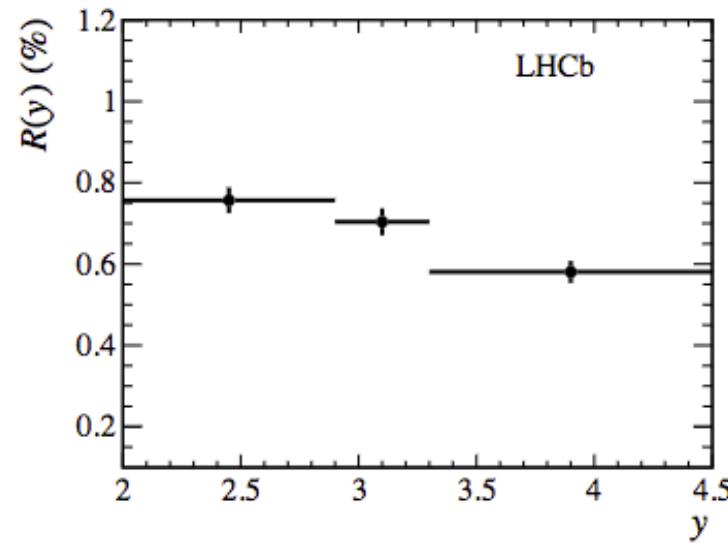
B_c production cross section

Measured at 8 TeV in the decay to J/ψ π⁺, and expressed as a ratio to B⁺ → J/ψ K⁺

$$R(p_T) = \frac{d\sigma(B_c)}{dp_T} BR(B_c \rightarrow J/\psi \pi) / \frac{d\sigma(B^+)}{dp_T} BR(B^+ \rightarrow J/\psi K)$$



$$R(y) = \frac{d\sigma(B_c)}{dy} BR(B_c \rightarrow J/\psi \pi) / \frac{d\sigma(B^+)}{dy} BR(B^+ \rightarrow J/\psi K)$$



The shapes agree with computations based on complete order- α_s^4

Phys. Rev. Lett. 114, 132001 (2015) ([arXiv:1411.2943](https://arxiv.org/abs/1411.2943))

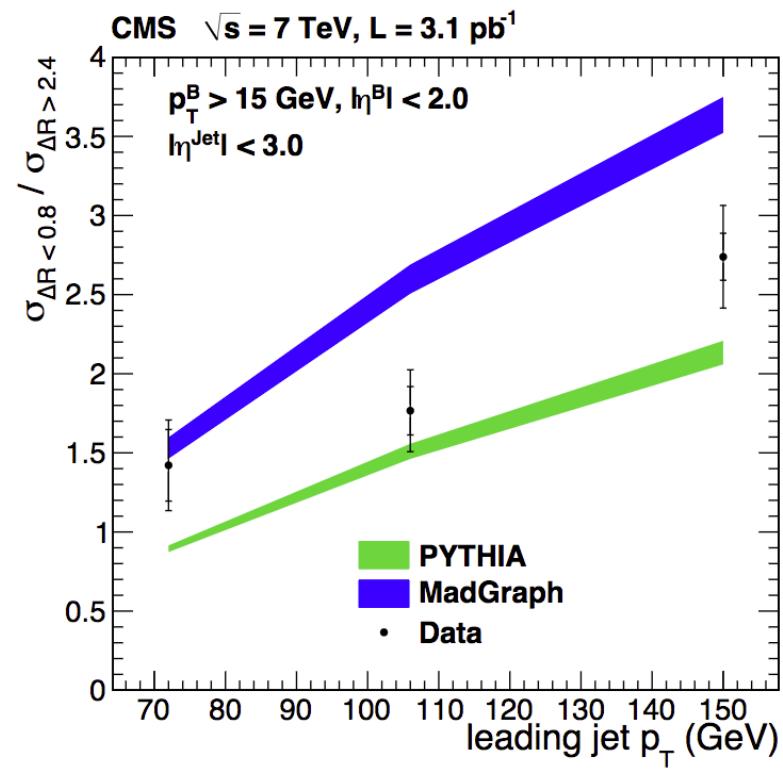
CMS result at 7 TeV: JHEP 01(2015) 063 ([arXiv:1410.5729](https://arxiv.org/abs/1410.5729))

Correlations in B-Bbar production

The effects of higher order diagrams are expected to become more visible in the kinematical correlations, in particular at small opening angle (contribution of the *gluon splitting* diagram).

First study on this subject by CMS:

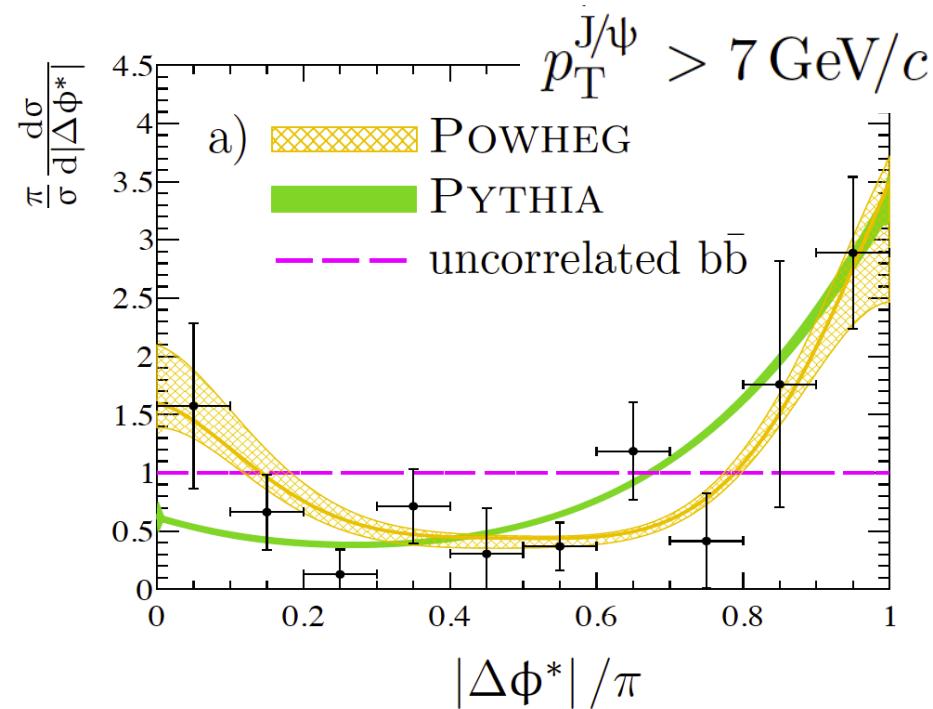
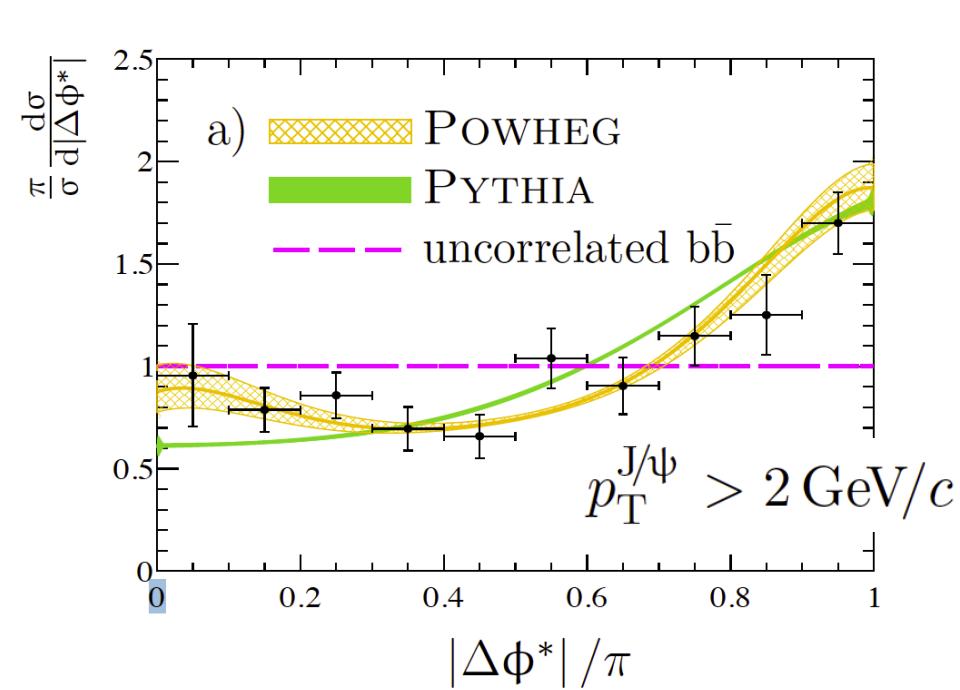
- Using B Bbar identified via secondary vertices. CMS found a significant small-angle (gluon splitting contribution).
- The data is not reproduced accurately by the generators, and appears to be in between MADGRAPH and PYTHIA. (JHEP 03 (2011) 136, [arXiv:1101.3194](https://arxiv.org/abs/1101.3194))



New result on B Bbar correlations from LHCb

Recent LHCb result (7+8 TeV): J/ψ are used a proxy for H_b through the inclusive decay $H_b \rightarrow J/\psi X$.

Comparison is made with POWHEG (NLO) and PYTHIA (LO).

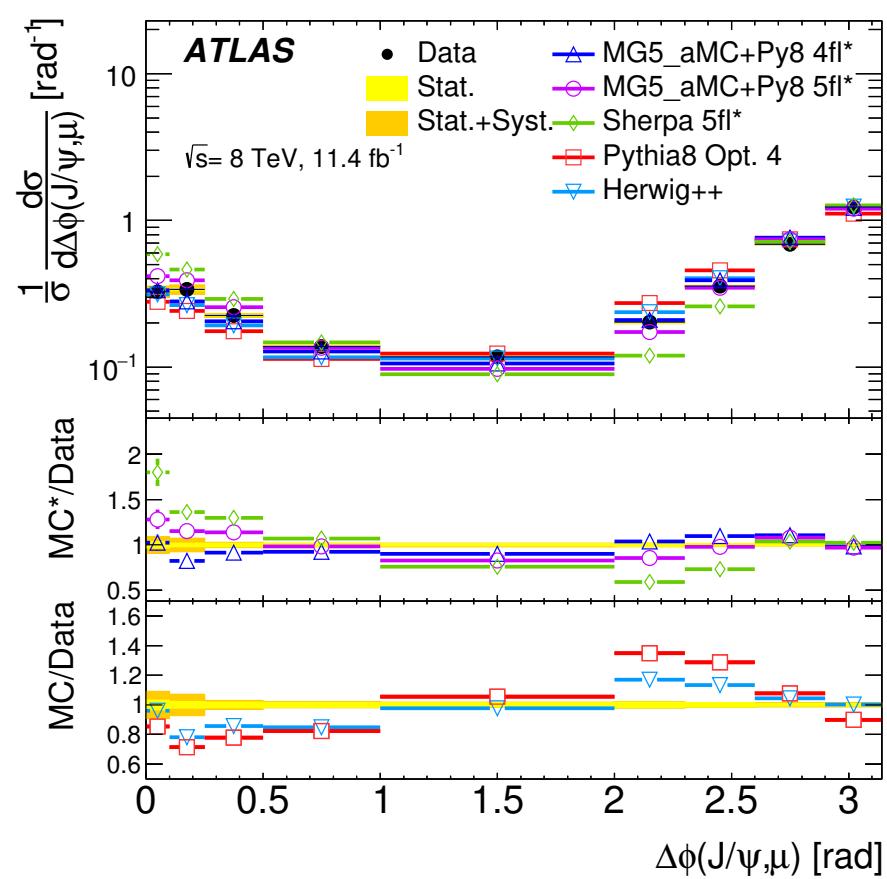
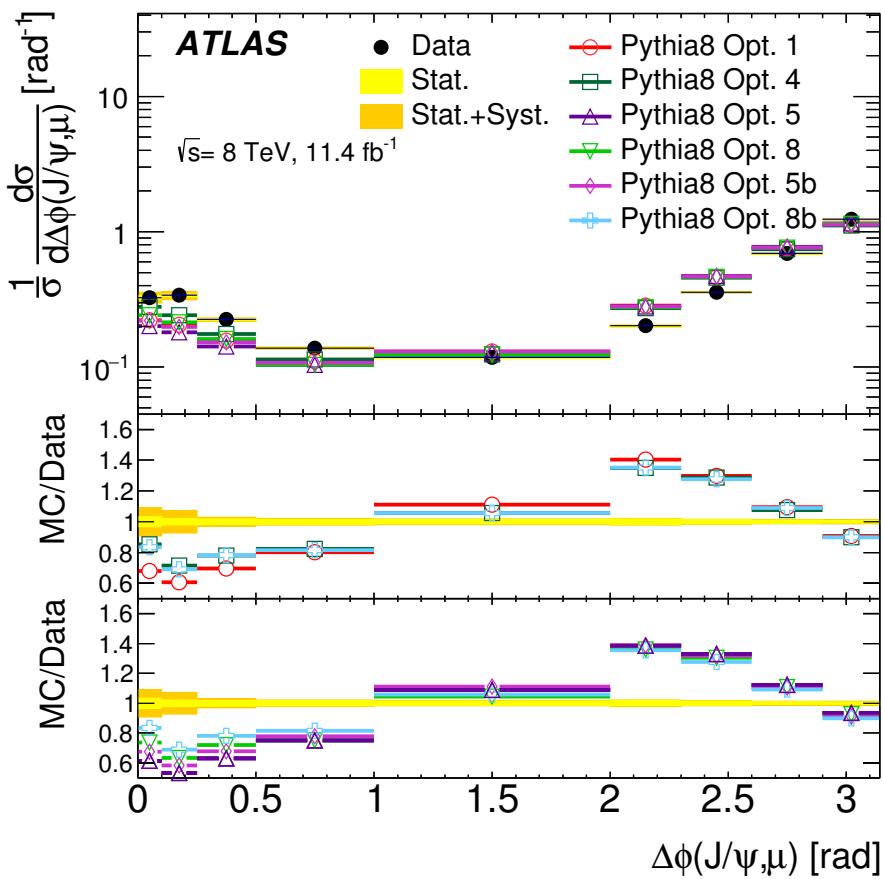


From this and other observables, the authors claim substantial agreement with either prediction.

[arXiv:1708.05994](https://arxiv.org/abs/1708.05994)

New result on B Bbar correlations from ATLAS

Here the B's are tagged through the decays to $J/\psi X$ and μ^\pm [arxiv:1705.03374](https://arxiv.org/abs/1705.03374).
 NLO computations appear generally more accurate than LO, with the 4-flavour MadGraph5_aMC@NLO+Pythia8 behaving better than others.



Quarkonia production: theoretical framework

Long-range, non perturbative effects enter for the production of a bound-state [Q-Qbar] : a *p*QCD approach is needed to cope with:

- Q and Qbar have to end up at nearly relative rest
- The final [QQbar] state is in a *color singlet* configuration

Models developed to include these requirements:

- **Color Evaporation Model:** $d\sigma_{[QQbar]}$ is related to $d\sigma_{Q, Qbar}$ for $2m_Q < m_{Q,Qbar} < 2m_{H(Q)}$, modulo a $1/N_{\text{colors}}$ factor.
- **Color Singlet Model (CSM):** here the *p*QCD hard scattering process is selected to include directly both requirements. The model is predictive to the extent of the required bound state wave function probability $|\Psi_{[QQbar]}|^2$, which can be extracted from decay widths.
- **The Non-Relativistic QCD approach (Color-Octet)** includes also diagrams with colored Q Qbar production. Long-Distance Matrix Elements to correct for this, via soft gluon exchange. LDMEs are typically extracted from fits to data. . .

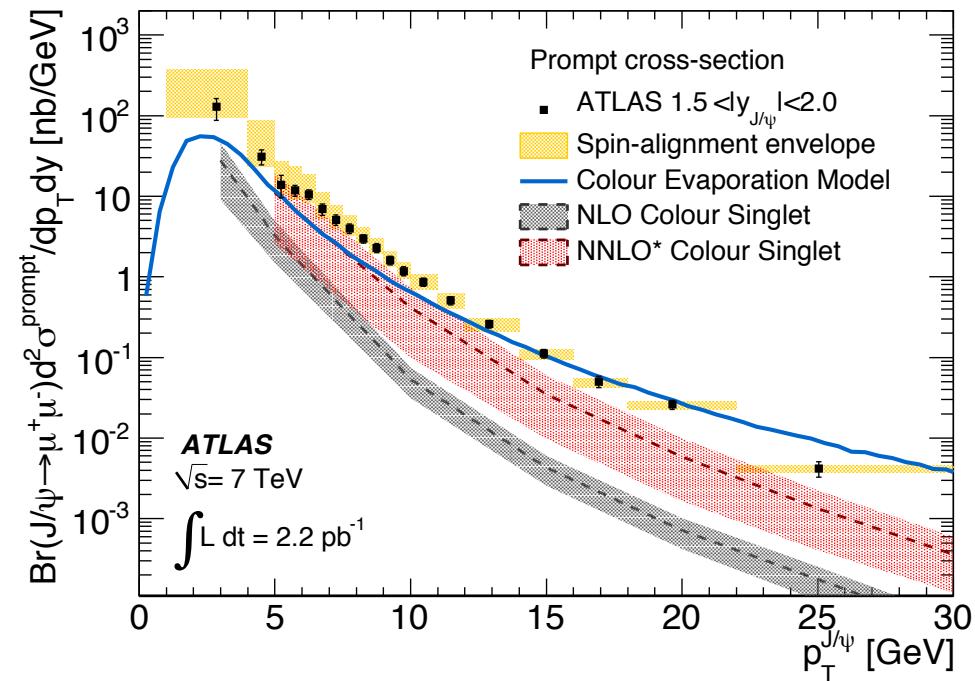
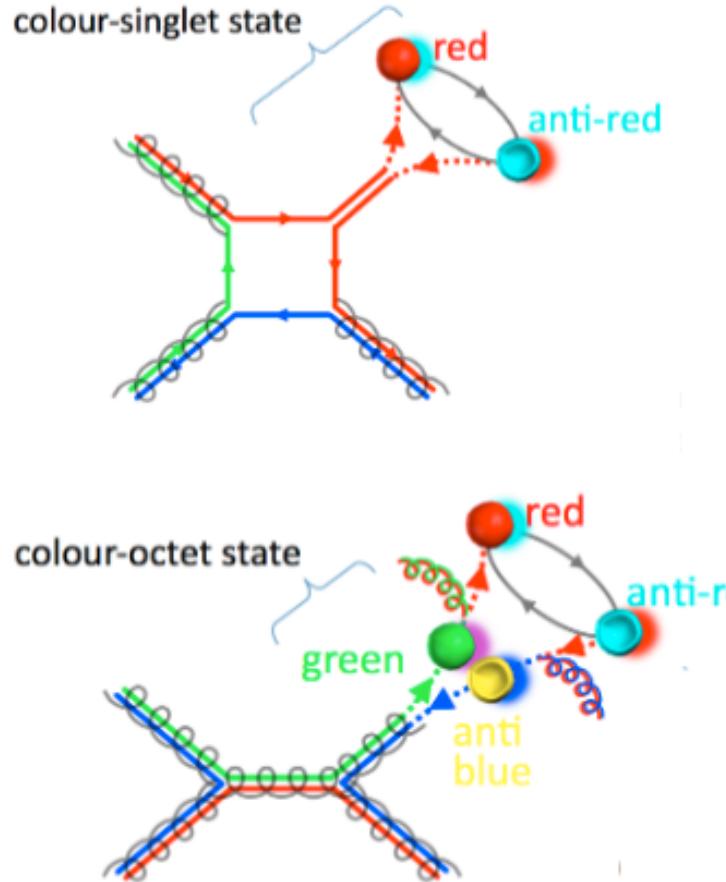
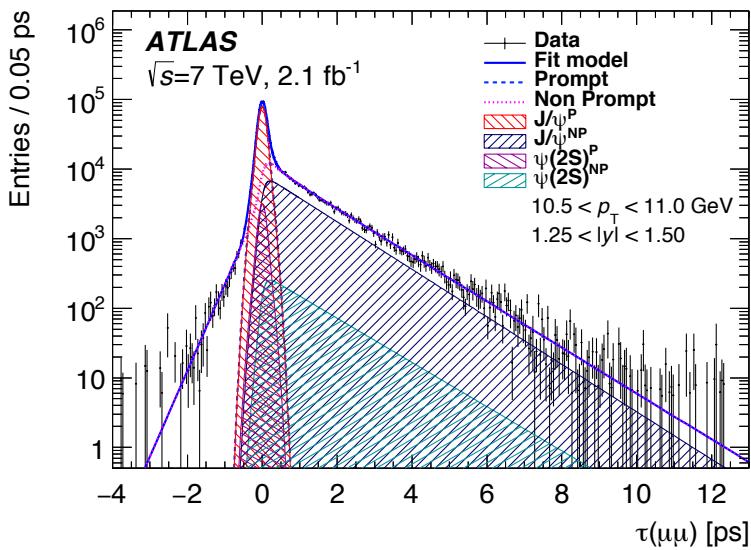
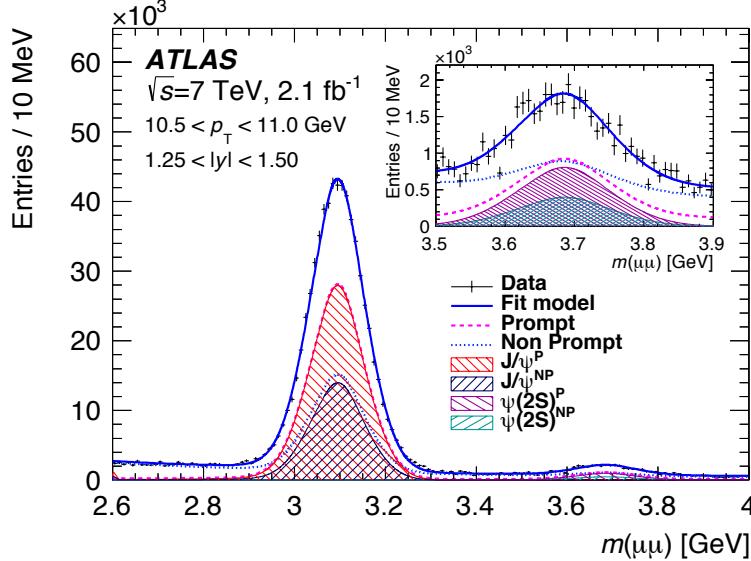


Illustration of CEM and CSM predictions for the differential production cross section of prompt J/ψ (Nucl.Phys. B850(2011) 387).

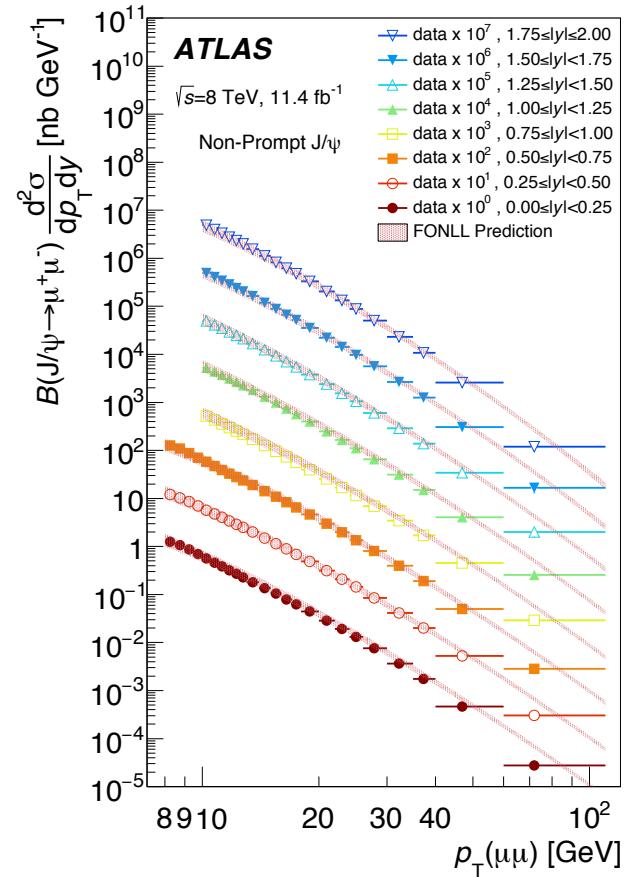
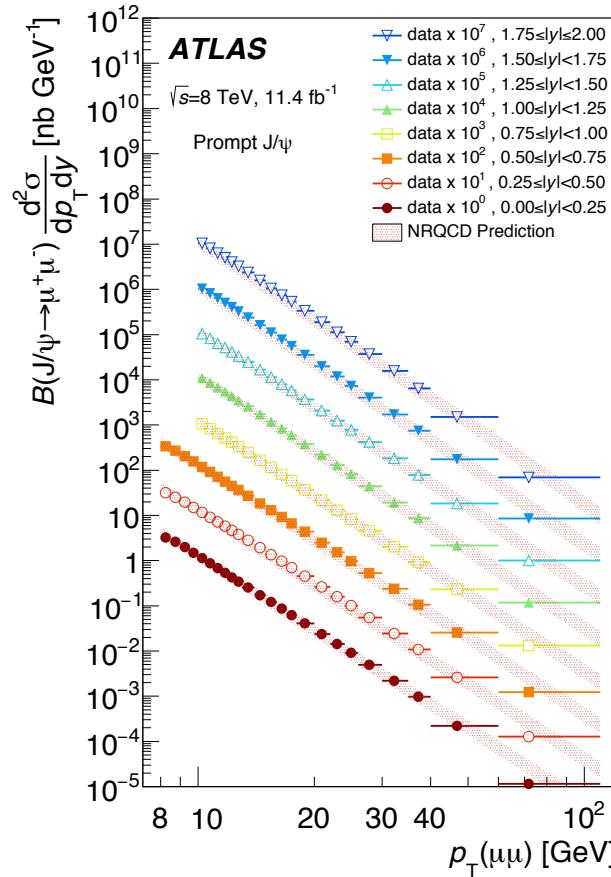
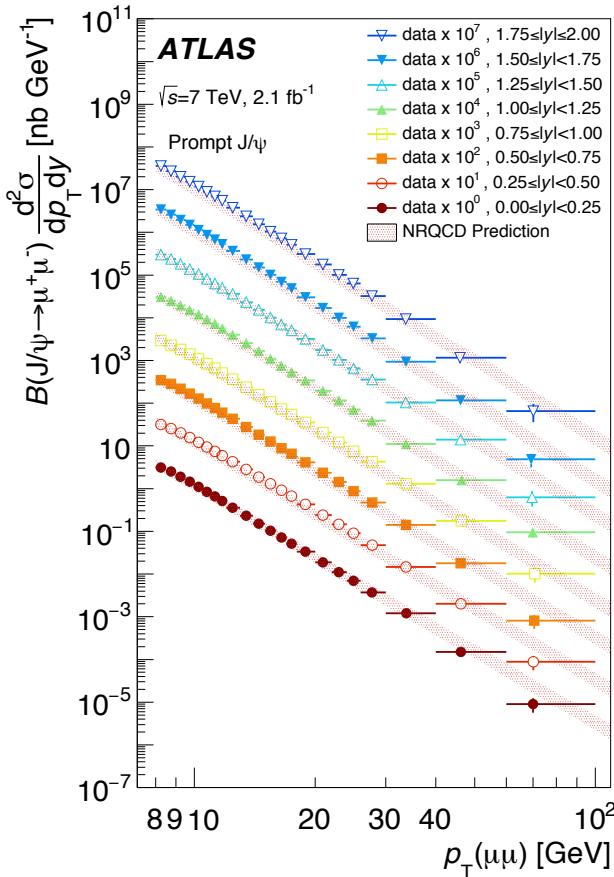
Experimental situation: prompt and non-prompt J/ ψ



Charmonium states are produced by two mechanisms with comparable contributions:

- **Prompt production:** the [QQbar] state is produced in the hard scattering process, with the muon pairs originating from the primary interaction
- **Non-prompt production:** the [QQbar] state is produced in the decay of a B hadron, with a decay vertex separated from the primary vertex.
- Prompt and non-prompt J/ψ , $\psi(2S)$ are identified with a simultaneous fit to the *mass and decay proper time* of the muon pair.

J/ ψ and $\psi(2S)$ production at 7, 8 TeV



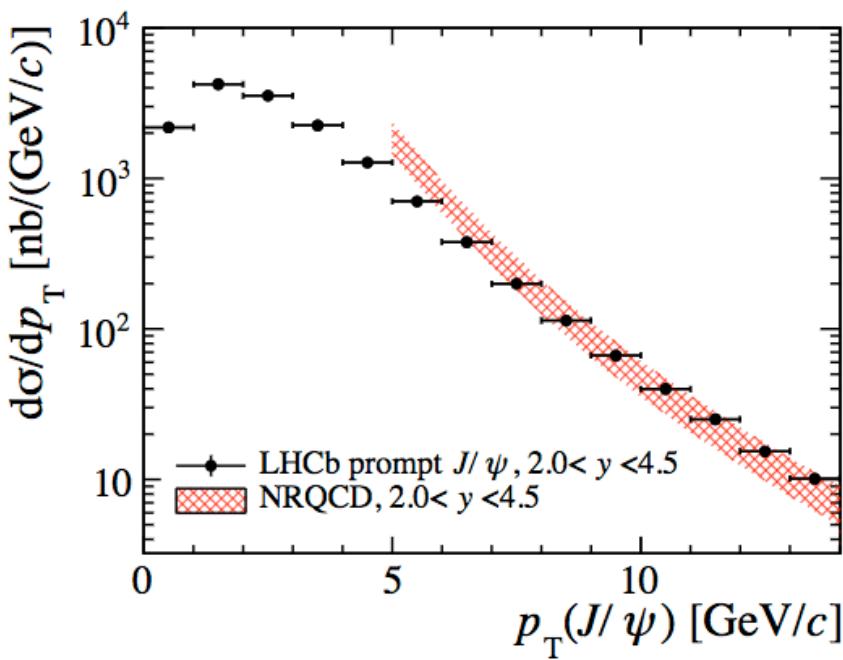
ATLAS: Eur. Phys. J. C76 (5) 1 (2016) [arXiv:1512.03657](https://arxiv.org/abs/1512.03657)
 (CMS, 7 TeV: PRL 114 (2015) 191802 [arXiv:1502.04155](https://arxiv.org/abs/1502.04155))

The measurements are in good agreement with predictions based on

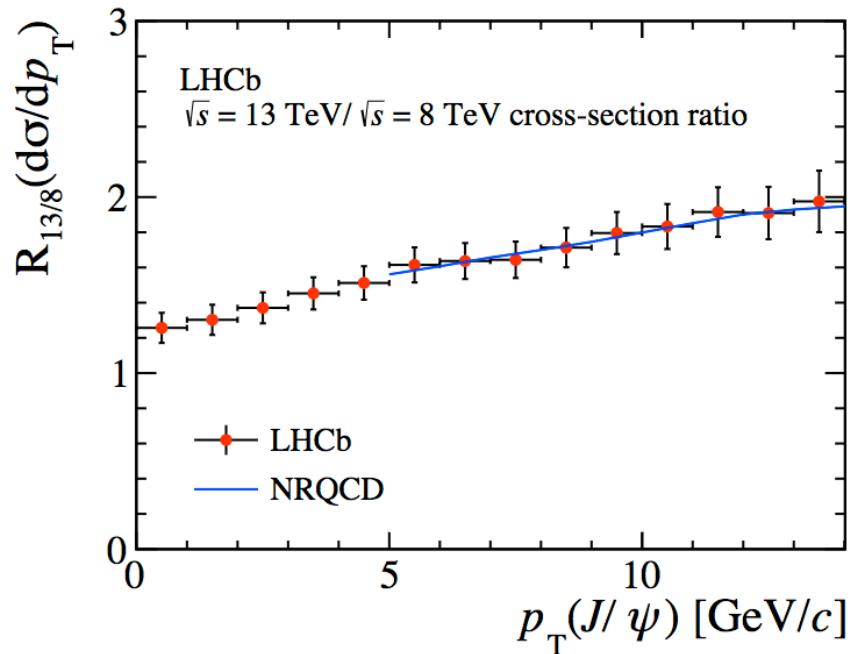
- NRQCD (for the prompt component)
- FONLL (non-prompt component)

Recent measurements of prompt J/ ψ from LHCb

Differential production cross section at 13 TeV



Cross section ratio between 13 and 8 TeV



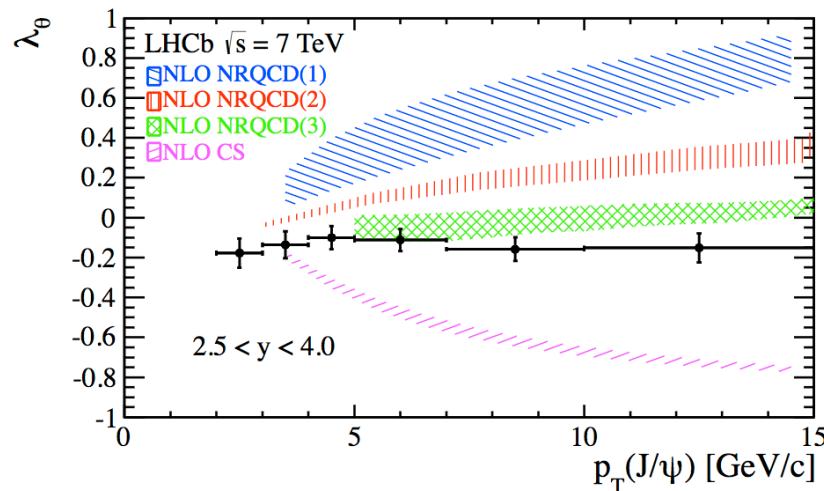
JHEP 10 (2015) 172 ([arXiv:1509.00771](https://arxiv.org/abs/1509.00771))

Preliminary results on J/ ψ , $\psi(2S)$, Y(nS) (n=1, 2, 3) at 13 TeV (2.4 fb^{-1}) in [CMS-PAS-BPH-15-005](https://cds.cern.ch/record/2180000)

Quarkonia polarization

Polarization observables:

- CSM predicts longitudinal polarization of the $J^P=1^-$ (J/ψ , Υ) states, at large p_T .
- NRQCD predicts that in the hadronization of the Q Qbar pair the different LDMEs produce different polarization (e.g. 3S_1 ^{octet} generates transverse polarization), with possibly significant transverse polarization (at large p_T)

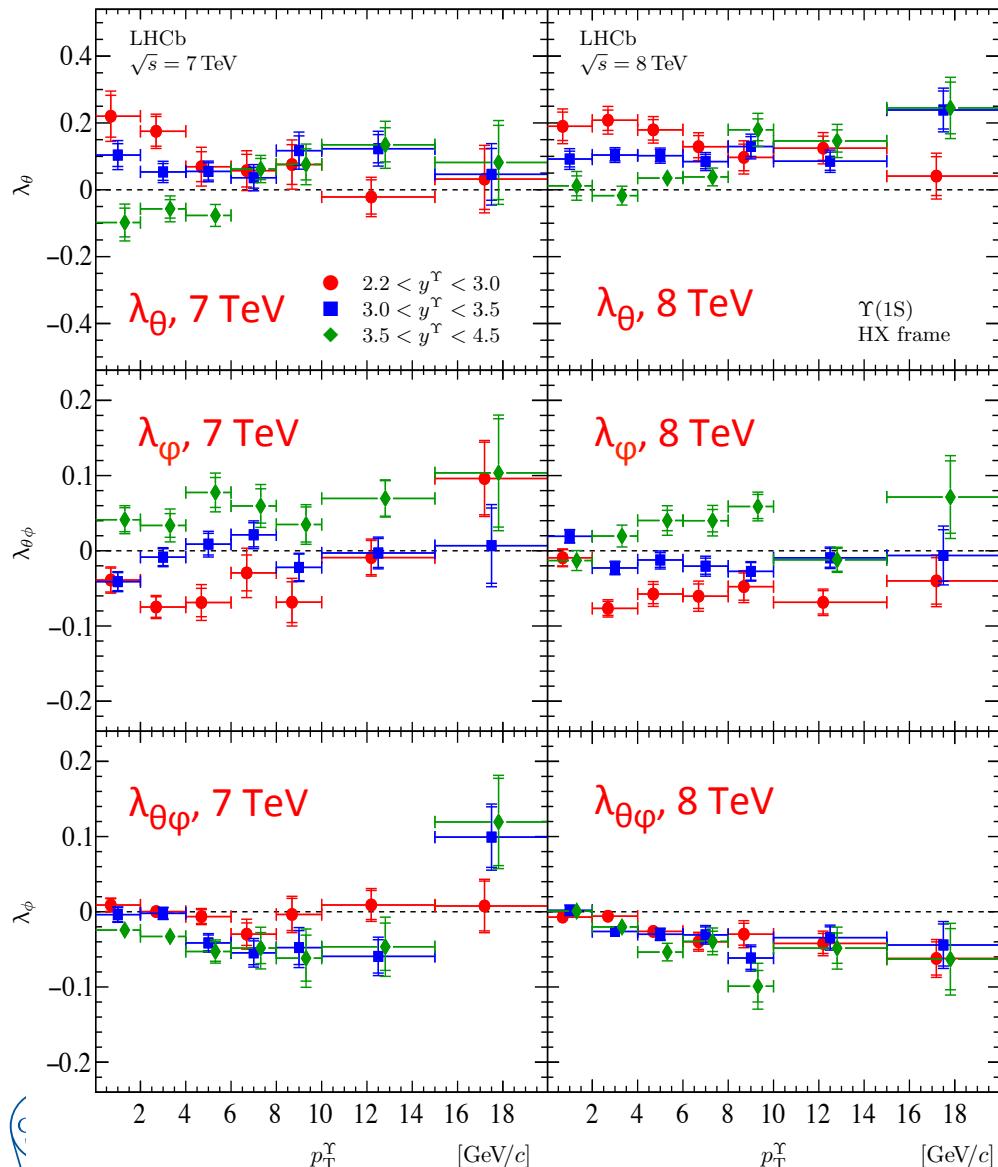


Eur.Phys.J. C 73, 11 (2013)
[arXiv:1307.6379](https://arxiv.org/abs/1307.6379)

$$dN/d\Omega = [1 + \lambda_\theta \cos^2\theta + \lambda_\phi \sin^2\theta \cos(2\phi) + \lambda_{\theta\phi} \sin(2\theta) \cos\phi] / (1 + \lambda_\theta/3)$$

For spin-1 state decaying to lepton pairs

Polarization of (prompt) quarkonia



All measurements so far have shown only small deviations from not polarized production.

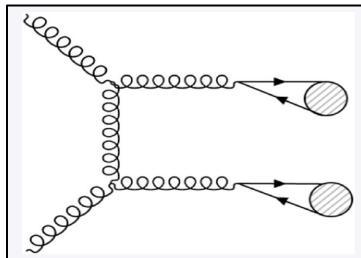
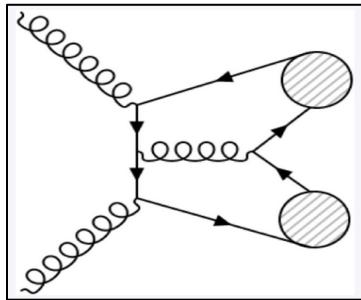
Here data from LHCb ([arXiv:1709.01301](https://arxiv.org/abs/1709.01301)): $\Upsilon(1S)$, $\Upsilon(2S)$ and $\Upsilon(3S)$ polarization (results provided in *helicity*, *Collins-Soper* and *Gottfried-Jackson* reference frames)

Similar conclusions reached by:

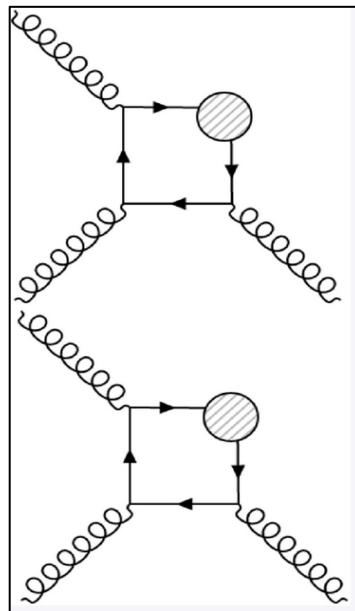
- CMS, for 7 TeV, $|y| < 1.2$, $p_T = 10-50$ GeV, PRL 110(2013) 081802 ([arXiv:1209.2922](https://arxiv.org/abs/1209.2922)),
- (CMS) $\Upsilon(1S)$, $\Upsilon(2S)$ in Phys.Lett. B 727 (2013) 381 ([arXiv:1307.6070](https://arxiv.org/abs/1307.6070)),
- LHCb for $\Upsilon(3S)$ in Eur.Phys.J. C (2014) 74:2872 ([arxiv:1403.1339](https://arxiv.org/abs/1403.1339))

Processes with associated production

- Studied as $J/\psi + J/\psi$, $J/\psi + W$, $J/\psi + Z$, $\gamma + \gamma$
- Two contributions to these processes:



Higher-order *real*
associated production
(Single Parton
Scattering, SPS)



Double Parton
Scattering (DPS)

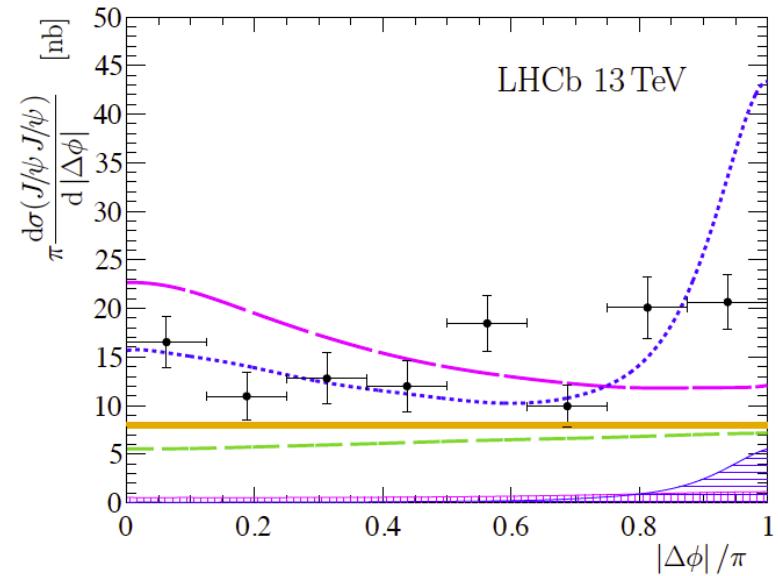
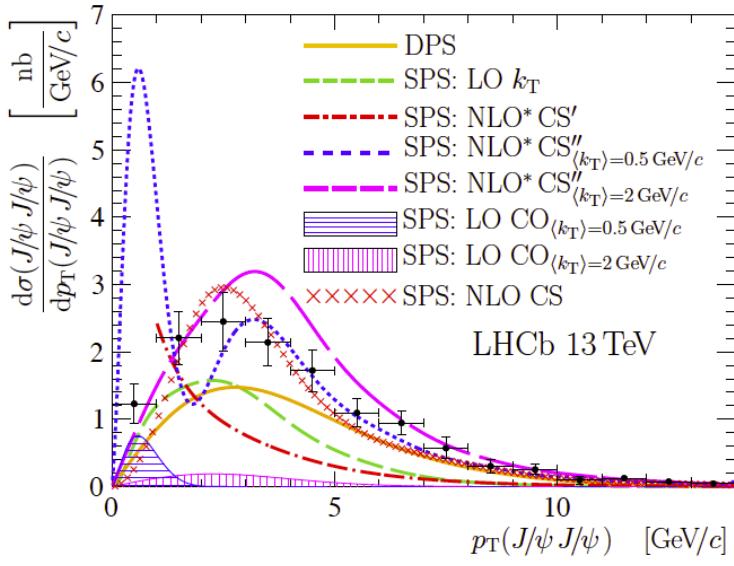
The *effective cross section* σ_{eff} for DPS (here for $J/\psi + J/\psi$):

$$\sigma_{\text{eff}} = \frac{1}{2} \left| \frac{\sigma_{J/\psi}^2}{\sigma_{\text{DPS}}} \right|$$

First observations of double J/ψ production at 7 TeV:

- LHCb (PL B707 (2012) 52)
- CMS (JHEP 09 (2014) 094.)

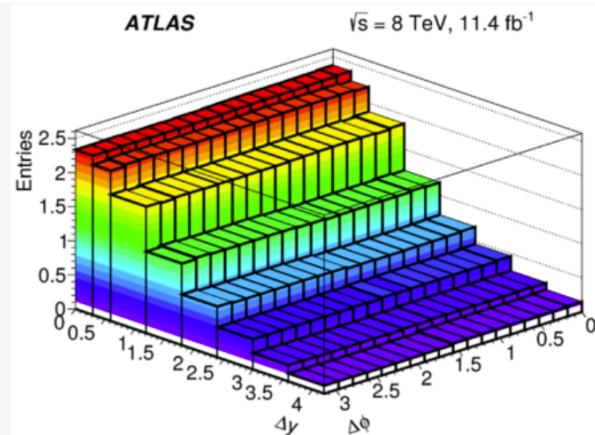
Recent result on $J/\psi J/\psi$ with LHCb



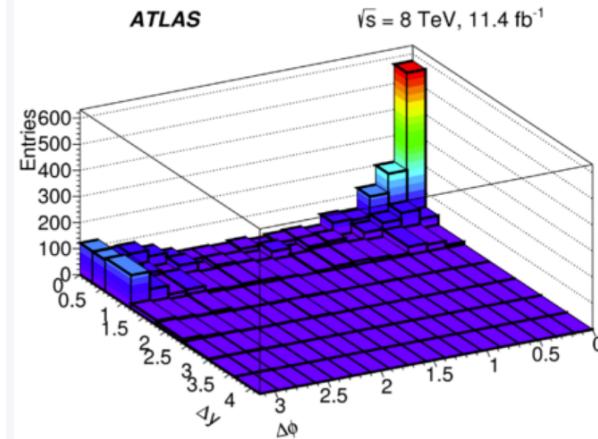
LHCb (JHEP 06 (2017) 047 ([arxiv:1612.07451](https://arxiv.org/abs/1612.07451)):

- Evidence of SPS and DPS contributions:
 - SPS compared with NRQCD and color-singlet/NLO predictions
 - DPS with σ_{eff} in the range 10.0 – 12.5 mb (model dependent).

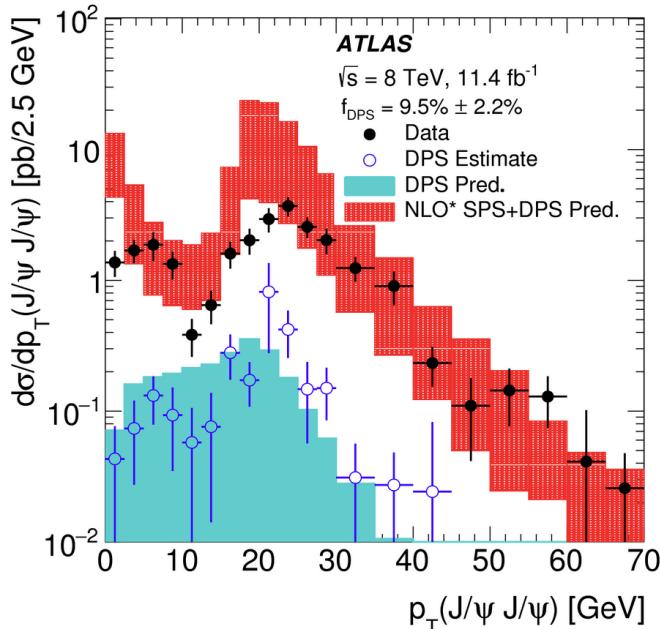
J/ ψ J/ ψ with ATLAS



Template for DPS obtained from random superposition of J/ ψ from different collisions.



SPS distribution from data after subtracting DPS (normalised in DPS dominated regions).

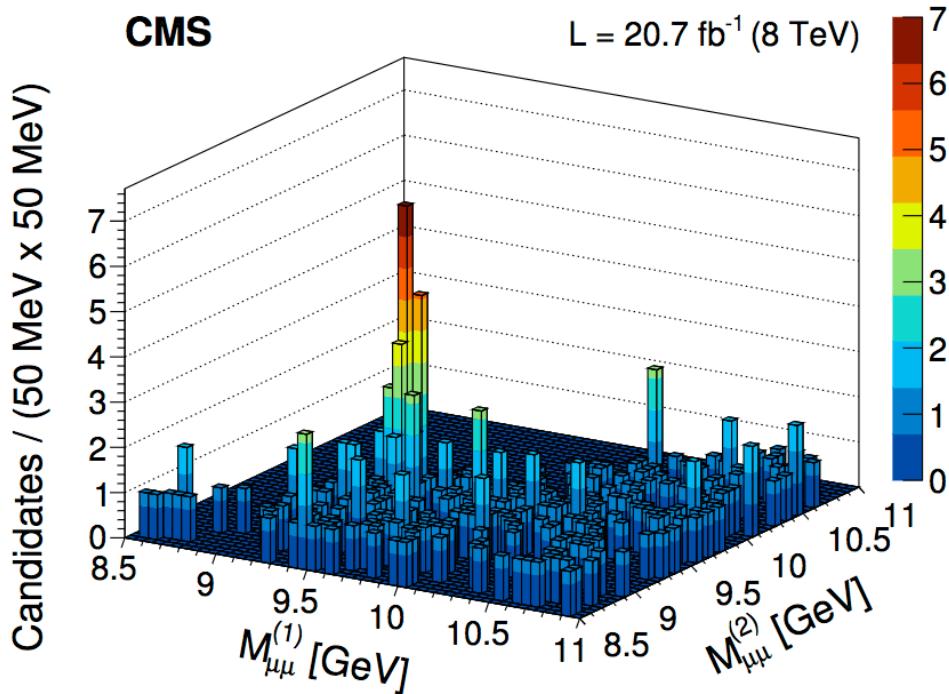


8 TeV data sample.

- SPS: a small-angle contribution is well visible. NLO color-singlet prediction provides a fair description of the result.
- SPS: $\sigma_{\text{eff}} = 6.3 \pm 1.6 \pm 1.0 \text{ mb}$

EPJ C77 (2017) 76, [arxiv:1612.02950](https://arxiv.org/abs/1612.02950)

Double Y production in CMS



38 ± 7 events of $\Upsilon(1S)\Upsilon(1S)$, corresponding to a fiducial production cross section $\sigma_{\text{fid}} = 68.8 \pm 12.7 \pm 7.4 \pm 2.8 \text{ pb}$ for $|\gamma(\Upsilon)| < 2.0$.

The result is in agreement with SPS calculations, together with a DPS contribution of about 10% to 30% of the total (which suggests $\sigma_{\text{eff}} \approx 2$ to 7 mb).

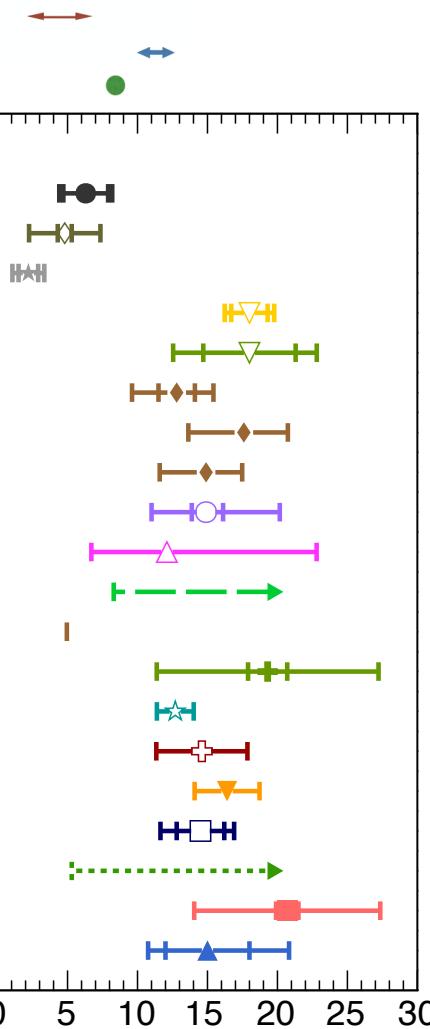
JHEP 05 (2017) 013, [arxiv:1610.07095](https://arxiv.org/abs/1610.07095)

σ_{eff} for double parton scattering

CMS ($\sqrt{s} = 8 \text{ TeV}$, $\Upsilon(1S) + \Upsilon(1S)$, 2016)

LHCb ($\sqrt{s} = 13 \text{ TeV}$, $J/\psi + J/\psi$, 2017)

CMS + Lansberg, Shao ($\sqrt{s} = 7 \text{ TeV}$, $J/\psi + J/\psi$, 2014)



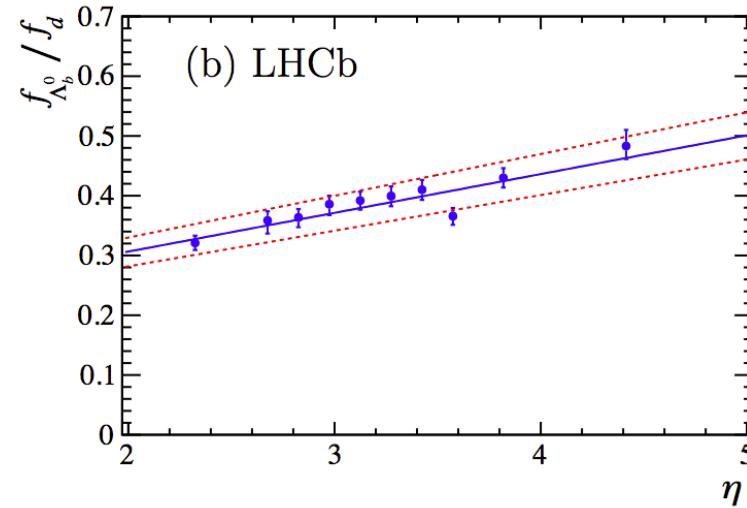
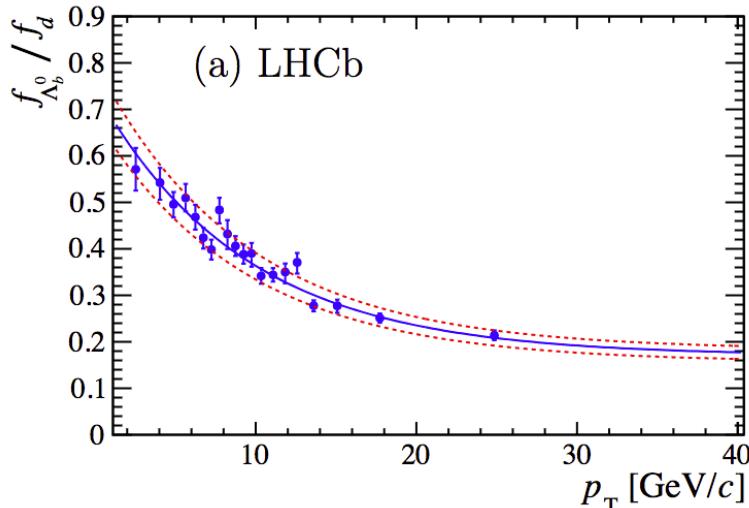
Is there evidence of non universality, with smaller values of σ_{eff} for quarkonia + quarkonia production ?

Conclusions

- The studies of the production of open heavy quark hadrons and of quarkonia in high energy collisions provide important tests of our understanding of the strong interactions.
- The range of the differential cross sections extends up to six order of magnitude across the p_T spectrum. Both central and forward production are studied.
- Substantial agreement is generally found between measurement and recent, detailed predictions. The experimental reach and accuracy underlines the relevance of computations at NLO, NNLO in some cases, NLL.
- Additional observables have been considered, including correlations in B Bbar production, quarkonia polarization, associated production.
- The increase in collision energy in LHC-Run 2, as well current and future increase in luminosity provide ground for further progress.

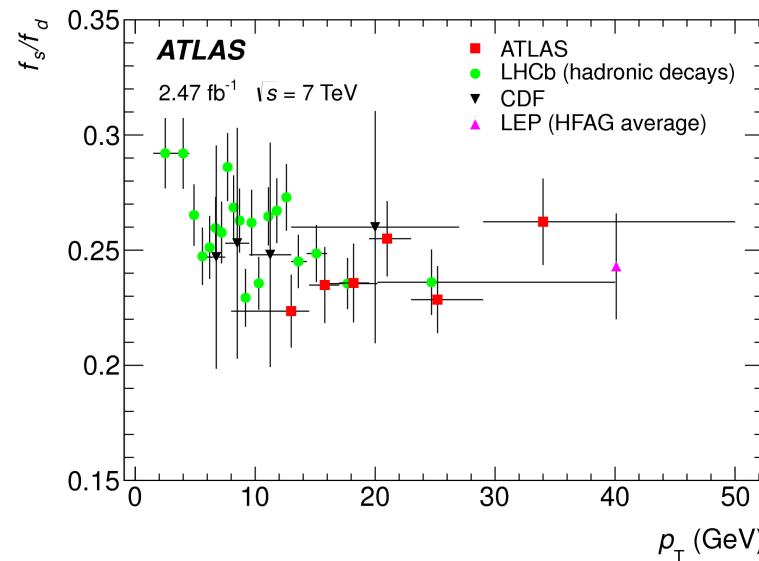
BACKUP AND AUXILIARY MATERIAL

Other results: production fractions

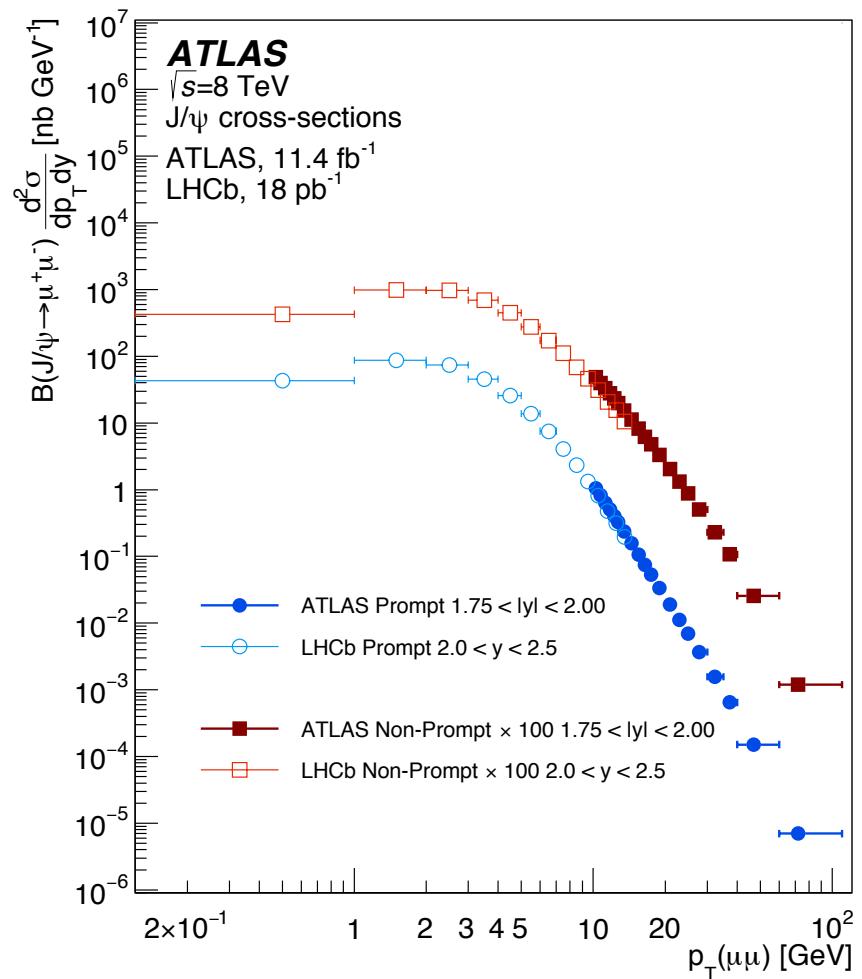
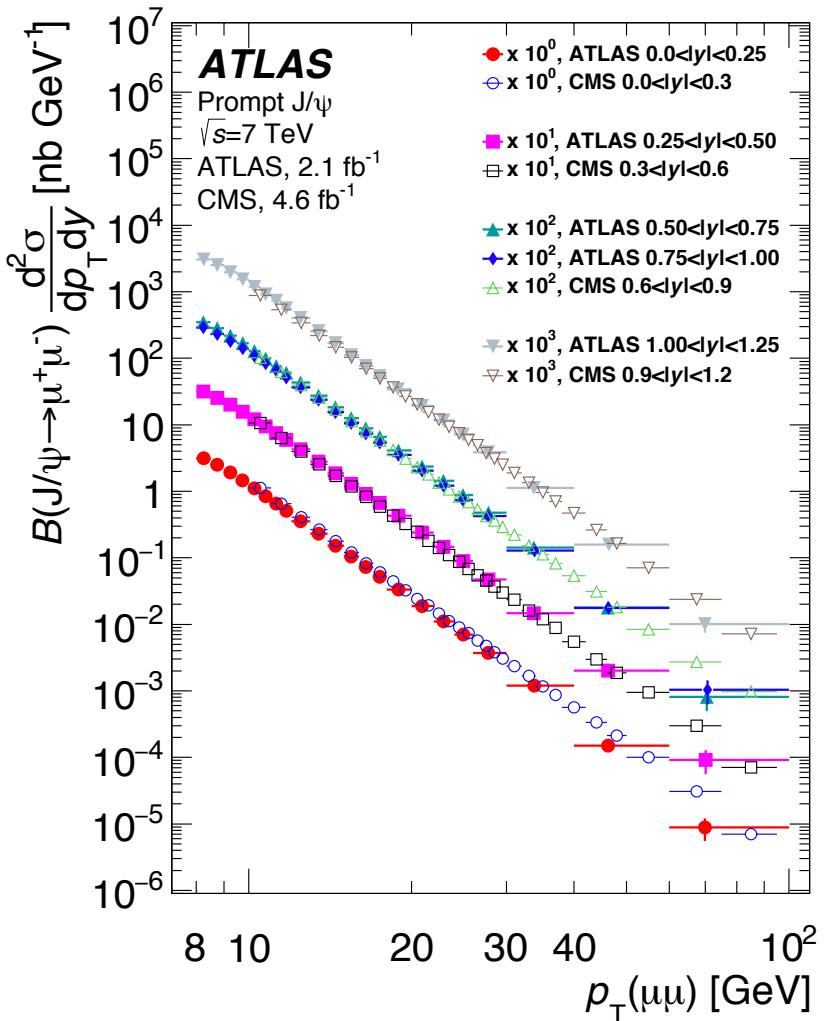


Baryon/meson production fraction measured by LHCb [JHEP 08(2014)143].

B_s^0/B^0 production ratio
 ATLAS: PRL 115, 262001(2015)
 LHCb: JHEP 04 (2013) 001



J/ ψ , $\psi(2S)$ production: comparisons among LHC experiments

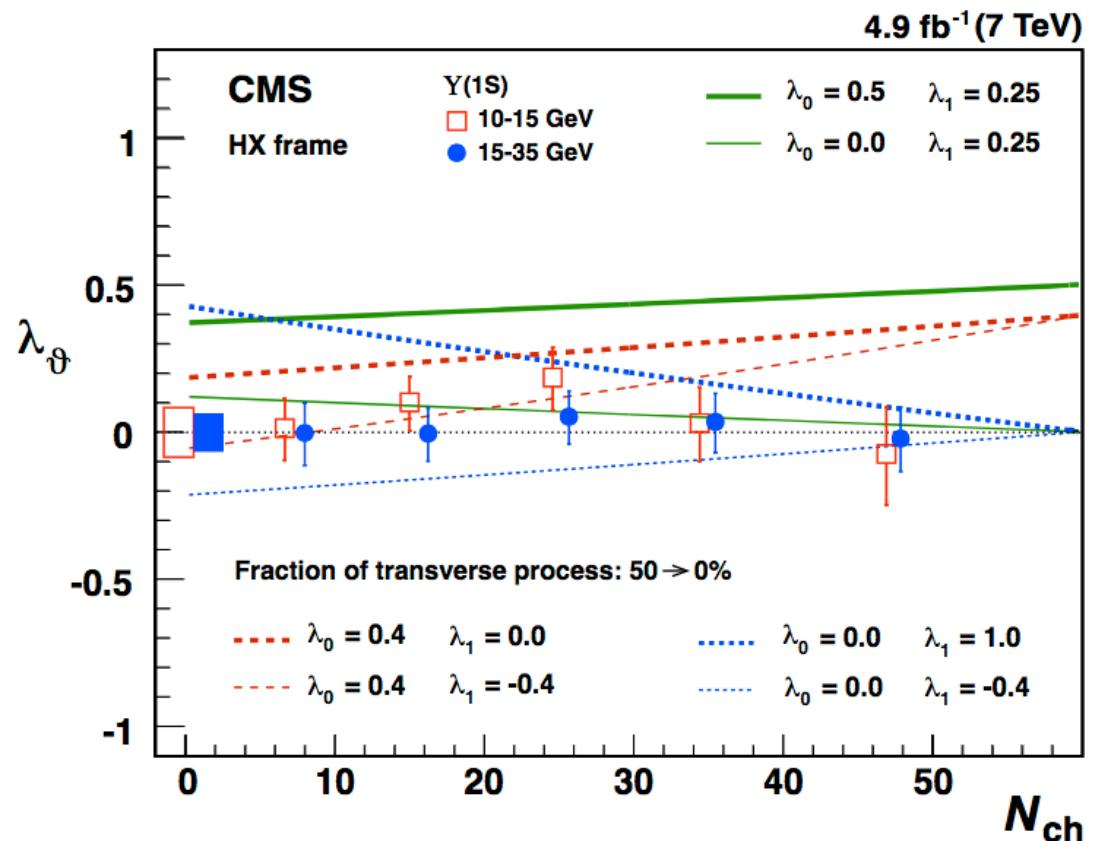


Υ polarization vs. particle multiplicity

CMS has tested a possible dependence of the polarization on the multiplicity of charged tracks ($|\eta| < 2.4$, $p_T > 500$ MeV), aiming at a correlation of the QQ hadronization process with the complexity of the hadronic environment.

No evidence of such dependence is found.

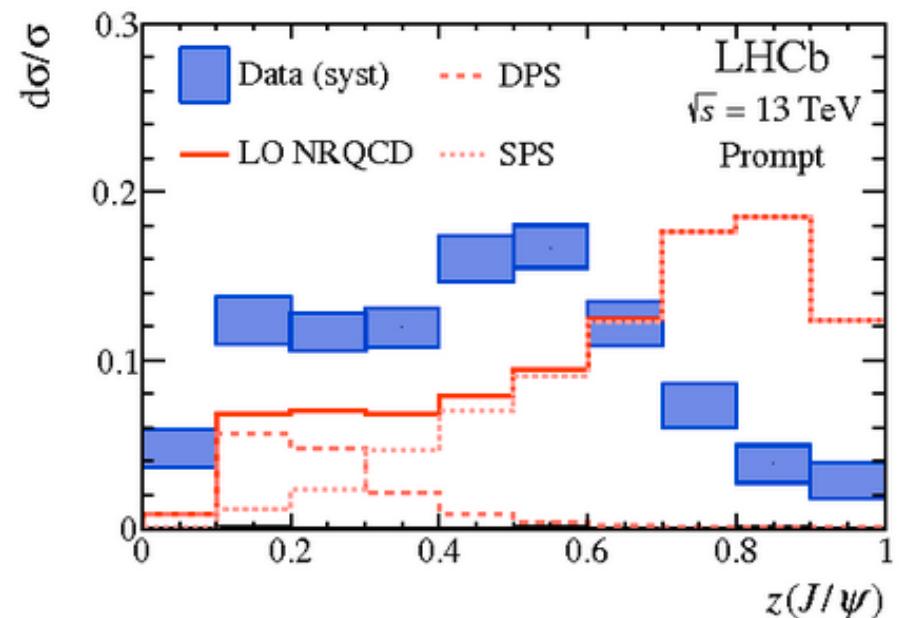
Phys.Lett. B 761 (2016) 31
[arXiv:1603.02913](https://arxiv.org/abs/1603.02913)



Prompt J/ ψ and associated jet

- The subject is interesting because it provides new observables for the production mechanism.
- Unfortunately the result of LHCb is for rather low p_T values (of Jet and of J/ ψ) and we do not have (yet) results from ATLAS or CMS.

- Phys.Rev.Lett. 118, 192001 (2017)
[arXiv:1701.05116](https://arxiv.org/abs/1701.05116)



More on quarkonia polarization

- The case considered more frequently is the decay of a spin 1 particle (e.g., J/ψ) into a lepton pair. In the vector rest frame, the angular distribution of the decay product is given by:

$$dN/d\Omega = [1 + \lambda_\theta \cos^2\theta + \lambda_\phi \sin^2\theta \cos(2\phi) + \lambda_{\theta\phi} \sin(2\theta) \cos\phi] / (1 + \lambda_\theta/3)$$

- The parameter are constrained to have absolute value less than 1 (actually, correlated constraints turn out to be tighter, see below).
- There is some freedom in the choice of the axes, normally chosen as:
 - The production plane is orthogonal to the y axis
 - Different choices are possible for the orientation of z and x , among the most common:
 - Helicity frame*: z along the momentum of the decaying particle in the laboratory frame
 - Collins-Soper* (CS) and *Gottfried-Jackson* (GJ) are among other possibilities



Polarization - 2

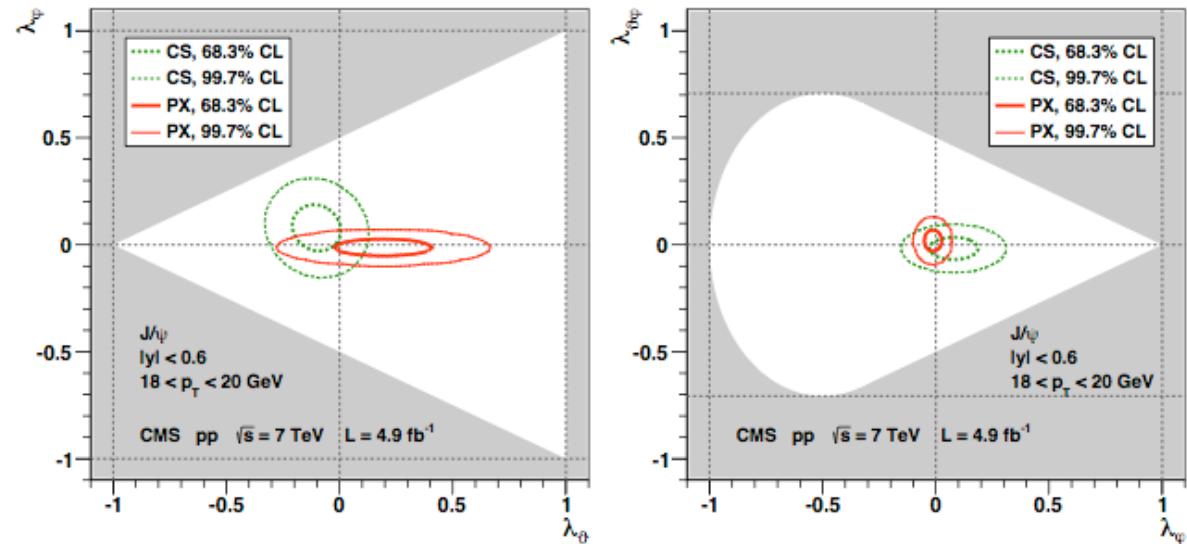
- All possible frames are related by a rotation about y , and corresponding transformations equation exists for the three coefficients.
- Therefore one could say that the physical polarization (or spin alignment), depends on two quantities rather than three (and in fact two independent *rotation invariant* quantities are known [*,\$]).
- Different computation may prefer different choices, of the coefficients, and it has been argued that model independent analyses could benefit from the determination of the invariant quantities.

[*] P. Faccioli et al., Phys. Rev. D 83 (211) 056008 ([arXiv:1102.3946](https://arxiv.org/abs/1102.3946)) and refs. therein,

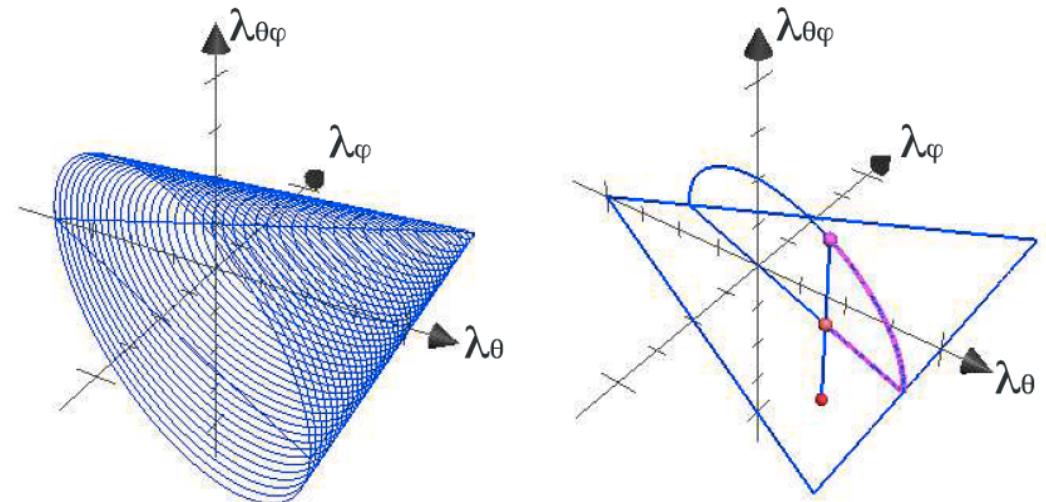
[§] S. P., Phys. Rev. D 83, 031503 ([arXiv:1012.2485](https://arxiv.org/abs/1012.2485)).

Polarization - 3

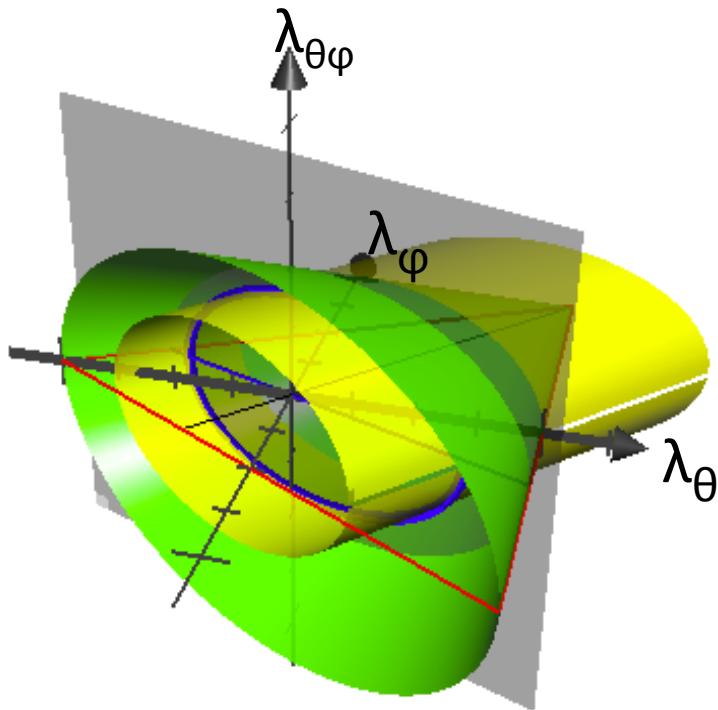
The boundaries on the values of the angular distribution parameters are often given on 2D projections (the grey area is forbidden).



A more complete picture is visible in 3D. For a rotation of frame the values of the parameters change following an ellipse that lies on a plane orthogonal to the λ_θ , λ_φ plane.



Polarization - 4



Geometrical description of the frame-invariant parameters of the angular distribution for J/ψ (Υ) decay to lepton pairs:

- A plane for the invariant in ref. [*],
- An elliptic cone for the invariant in ref. [§].

The intercepted ellipsis defines the set of values of the angular distribution parameters linked by a different choice of reference frame.



List of recent HQ production results at LHC: LHCb

- LHCb Y production at 7, 8 TeV: <http://arxiv.org/abs/1509.02372>
- LHCb J/psi production at 13 TeV : <http://arxiv.org/abs/1509.00771>
- LHCb associated Y and open charm at 7, 8 TeV:
<http://arxiv.org/abs/1510.05949>
- LHCb Lambda_b and B0bar production ; <http://arxiv.org/abs/1509.00292>]
- LHCb Y exclusive production cross section at 7 TeV:
<http://arxiv.org/abs/1505.07024>
- LHCb eta_c production : <http://arxiv.org/abs/1409.3612>
- LHCb $\chi b 1(1P)$ and $\chi b 2(1P)$ relative production:
<http://arxiv.org/abs/1409.1408>
- LHCb χb production at 7, 8 TeV : <http://arxiv.org/abs/1407.7734>
- LHCb pair of charmonium (produced exclusively?) :
<http://arxiv.org/abs/1407.5973>
- LHCb kinematic dependence of Lambda_b production:
<http://arxiv.org/abs/1405.6842>



LHCb results continued

- LHCb $\psi(2S)$ polarisation at 7 TeV : <http://arxiv.org/abs/1403.1339>
- LHCb polarisation and helicity amplitudes in $\Lambda_b \rightarrow \Lambda J/\psi$:
<http://arxiv.org/abs/1302.5578>
- LHCb Y polarization at 7, 8 TeV <http://arxiv.org/abs/1709.01301>
- B Bbar correlations <http://arxiv.org/abs/1708.05994>
- Production asymmetries in $B^0, B^0_s, B^+ \Lambda_b$ at 7, 8 TeV
<http://arxiv.org/abs/1703.08464>
- J/ψ prompt production in jets <http://arxiv.org/abs/1701.05116> PRL 118, 192001 (2017)
- Prompt J/ψ pair production at 13 TeV <http://arxiv.org/abs/1612.07451> JHEP 2017:47 (June 2017)



CMS recent results on HF production

- Υ pairs production: [BPH-14-008](#) JHEP 05 (2017) 013
- Total and differential B^+ cross section at 13 TeV [PLB 771 \(2017\) 435](#)
- J/ψ and $\psi(2S)$ at 7 TeV [BPH-14-001](#) PRL 114 (2015) 191802
- $\Upsilon(1S-3S)$ production at 7 TeV [BPH-12-006](#) PLB 749 (2015) 14
- B_c/B^+ cross section at 7 TeV [BPH-12-011](#) JHEP 01 (2015) 063
- $\chi_{b2}(1P)/\chi_{b1}(1P)$ at 8 TeV [BPH-13-005](#) PLB 743 (2015) 383
- J/ψ pair productioon [BPH-11-021](#) JHEP 09 (2014) 094
- J/ψ and $\psi(2S)$ polarization at 7 TeV [BPH-13-003](#) PLB 727 (2013) 381



ATLAS results on HF production

- B Bbar correlation in J/ ψ +mu <https://arxiv.org/abs/1705.03374>
- J/ ψ + J/ ψ at 8 TeV [Eur. Phys. J. C77\(2017\)76](#)
- J/ ψ + Z at 8 TeV [Eur. Phys. J. C75 \(2015\) 229](#)
- J/ ψ and $\psi(2S)$ production at 7, 8 TeV [Eur. Phys. J. C 76 \(5\) 1-47 \(2016\)](#)
- $X(3872)$ production at 8 TeV [JHEP01\(2017\)117](#)
- Fragmentation ratio f_s/f_d [Phys.Rev.Lett.115.262001](#)
- J/ ψ $\pi\pi$ production at 7 TeV [JHEP09\(2014\)079](#)
- χ_{c1}, χ_{c2} production at 7 TeV [JHEP07\(2014\)154](#)
- $D^\pm, D^{*\pm}, D_s^+$ production at high pT at 7 TeV [Nucl. Phys. B 907 \(2016\) 717](#)
- J/ ψ +W production at 7 TeV [JHEP04\(2014\)172](#)
- B+ cross section [JHEP10\(2013\)042](#)
- Υ cross section at 7 TeV [Phys. Rev. D 87, 052004 \(2013\)](#)
- B cross section from $D^*\mu$ events [Nucl. Phys. B 864 \(2012\) 341](#)

Some additional references

Bc differential cross section, agreement in shape in with computations based on a complete order- α_s^4 :

- *C.H Chang et al. PR D48 (1993) 4086 and PL B364(1995)78,*
- *Berezhnoy et al. Phys. Atom. Nucl 58 (1995) 672,*
- *Kolodziej et al. PL B355(1995)337*

Predictions for polarization of prompt J/ ψ 's in NRQCD NLO computations:

M. Butenschoen and B. A. Kniehl, *J/ ψ polarization at Tevatron and LHC: Nonrelativistic-QCD factorization at the crossroads*, [Phys. Rev. Lett. 108 \(2012\) 172002](#), [arXiv:1201.1872](#).

B. Gong, L.-P. Wan, J.-X. Wang, and H.-F. Zhang, *Polarization for prompt J/ ψ , $\psi(2S)$ production at the Tevatron and LHC*, [Phys. Rev. Lett. 110 \(2013\) 042002](#), [arXiv:1205.6682](#).

K.-T. Chao et al., *J/ ψ polarization at hadron colliders in nonrelativistic QCD*, [Phys. Rev. Lett. 108 \(2012\) 242004](#), [arXiv:1201.2675](#); H.-S. Shao and K.-T. Chao, *Spin correlations in polarizations of P-wave charmonia χ_{cJ} and impact on J/ ψ polarization*, [arXiv:1209.4610](#).